



The Tai Chi of Basic Mathematics

(An attempt to find balance)

In 1960, I was an SMSG (School Mathematics Study Group) product, and mathematics enlightened me. Although we're no longer racing to the moon, maybe it is time to reflect on the direction we are taking basic mathematics. Our goal is similar, to raise the standards of our students. In this case, so that they can compete globally.

The I-Ching (Book of Changes) from which the symbol above comes, recognizes the dynamic balance of opposites, looks at the various means for change, and the acceptance that change is inevitable.

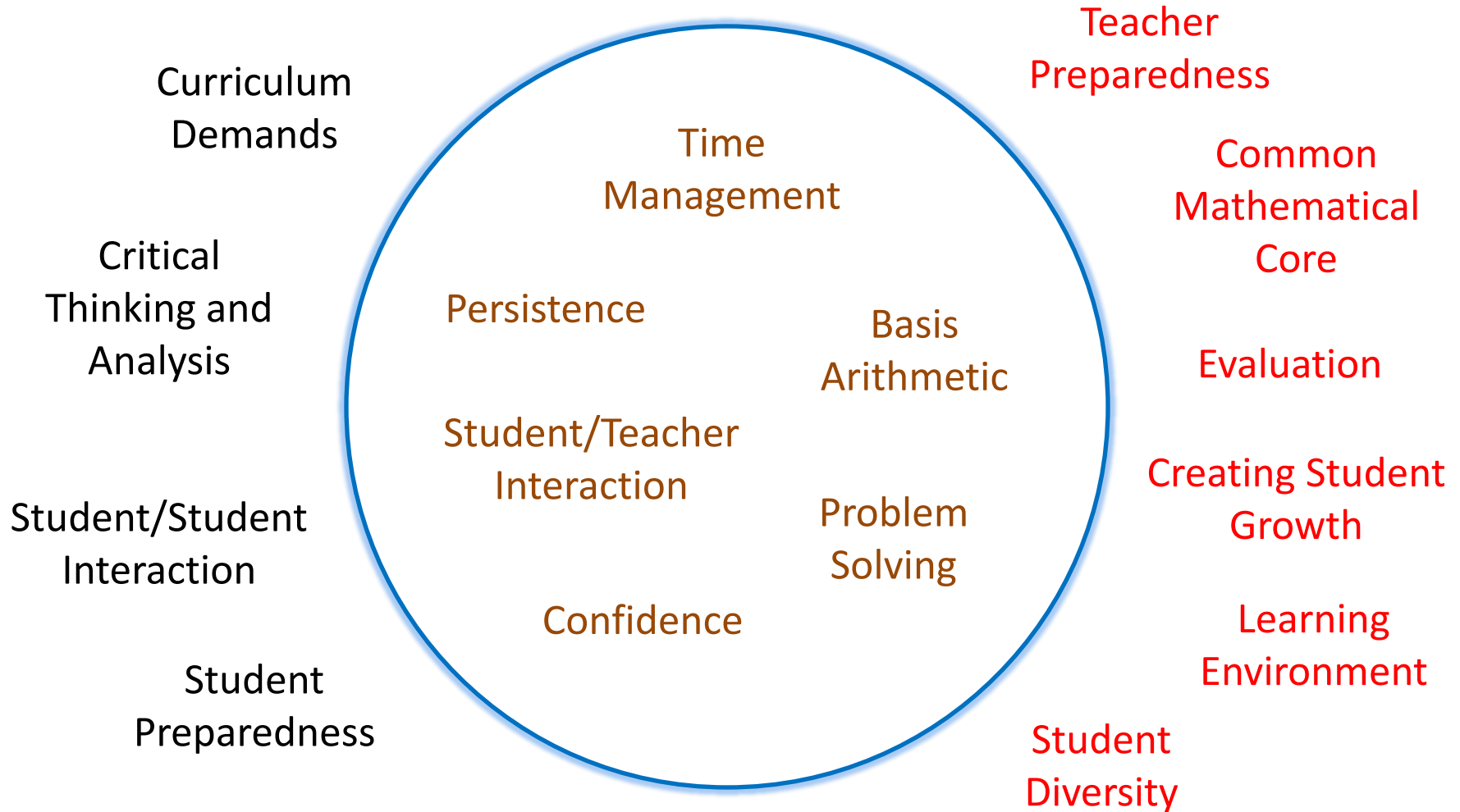


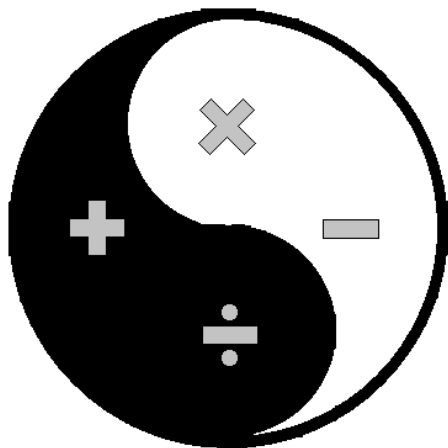
See, the only thing missing is my tie!



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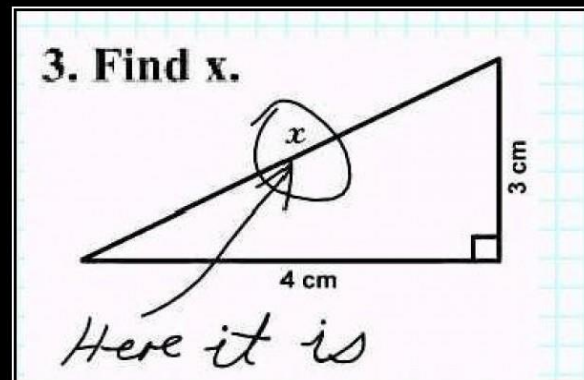
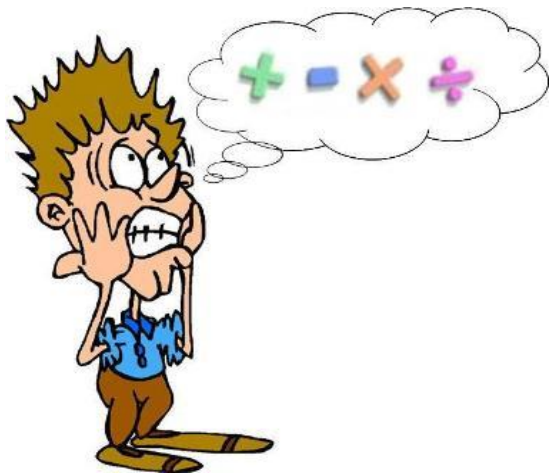




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Looking at our students.

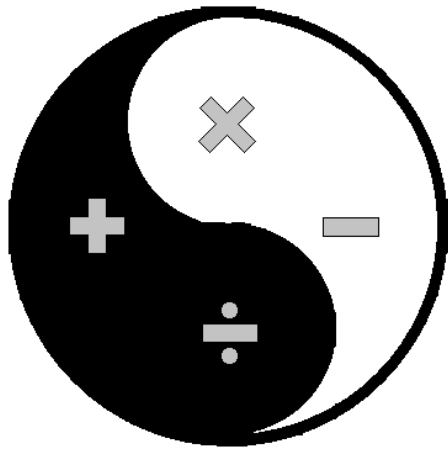


SIMPLICITY

The simplest solutions are often the cleverest
They are also usually wrong

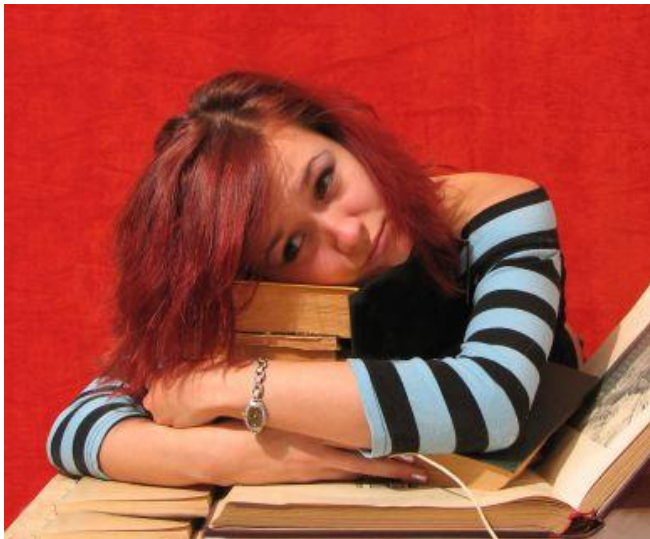
"I always did poorly in math, so why bother studying. But I need this class for my major, and it's my third time."

"This stuff is too easy for me!" I don't need to study. I'm in the wrong class. Can I leave class early to study for Biology? Biology is a pre-Med requirement."



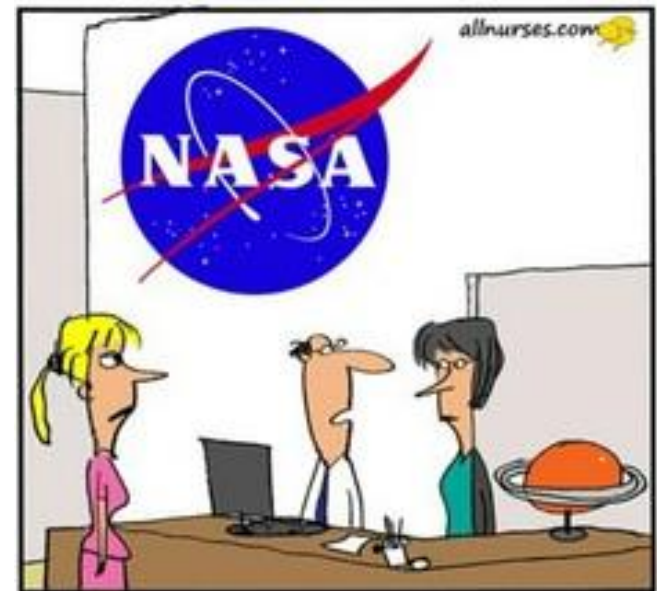
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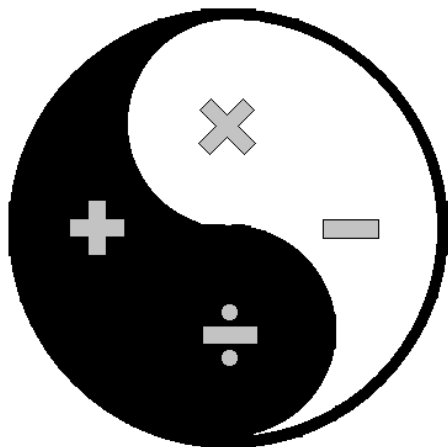
Those students with math anxiety may find some success in returning to the fundamentals, but applications and making the connections is still difficult. Over-confident students have realized that they may not moving on.

About a Nursing Student



"She's a nursing student who also works. She wants to know if we could alter the earth's rotation to make the days longer. Apparently, she needs more time."

This student is in trouble.



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Looking at the curriculum.

DRILL and PRACTICE.

Add.

1. $8 + 36$	2. $46 + 5$	3. $5 + 7 + 8$
4. $3 + 9 + 7$	5. $2 + 7 + 5 + 3$	6. $6 + 5 + 8 + 9$
7. $\begin{array}{r} 792 \\ + 36 \\ \hline \end{array}$	8. $\begin{array}{r} 3099 \\ + 8764 \\ \hline \end{array}$	
9. $9674 + 2091 + 450$	10. $10,346 + 9807 + 123$	
11. $8 + 3 + 86$	12. $370,816 + 2115 + 92 + 348$	
13. $\begin{array}{r} 60,675 \\ + 86,501 \\ \hline \end{array}$	14. $\begin{array}{r} 66,177 \\ + 9,323 \\ \hline \end{array}$	
	$\begin{array}{r} 50,689 \\ + 7,135 \\ \hline \end{array}$	

15. Mr. Maguire purchases these items at the supermarket.

Beef	\$18
Potatoes	\$ 3
Dog food	\$ 5
Beer	\$ 6

What is the total cost?

16. What is the total length of this shaft?

$\begin{array}{c} \text{---} 68 \text{ cm ---} 72 \text{ cm ---} 49 \text{ cm ---} \end{array}$

17. Ms. Nichols had \$915 in her checking account. She deposited \$97 in the account. What is her balance now?

18. Ross weighed 176 pounds before going on his vacation. He gained 14 pounds on his trip. What did Ross weigh after his vacation?

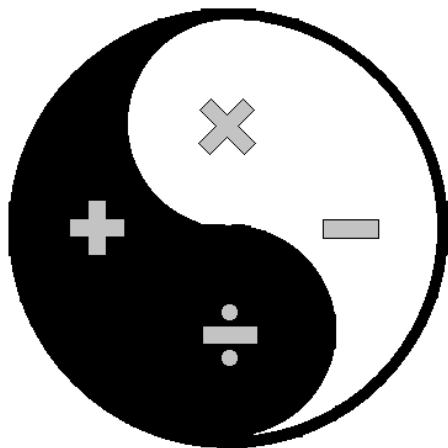
Subtract. Check your answers by adding.

19. $43 - 5$	20. $759 - 42$	21. $638 - 46$	22. $\begin{array}{r} 2367 \\ - 124 \\ \hline \end{array}$
23. $\begin{array}{r} 4238 \\ - 1705 \\ \hline \end{array}$	24. $\begin{array}{r} 72,378 \\ - 6,084 \\ \hline \end{array}$	25. $\begin{array}{r} 3107 \\ - 783 \\ \hline \end{array}$	26. $\begin{array}{r} 6324 \\ - 583 \\ \hline \end{array}$
27. $\begin{array}{r} 64,013 \\ - 4,208 \\ \hline \end{array}$	28. $\begin{array}{r} 6004 \\ - 36 \\ \hline \end{array}$	29. $\begin{array}{r} 50,026 \\ - 1,451 \\ \hline \end{array}$	30. $700 - 8$
31. $300 - 67$	32. $5000 - 407$	33. $6000 - 1038$	34. $8000 - 350$
35. $70,000 - 300$	36. $\begin{array}{r} 200,300 \\ - 7,502 \\ \hline \end{array}$	37. $\begin{array}{r} 520,036 \\ - 71,578 \\ \hline \end{array}$	38. $\begin{array}{r} 308,010 \\ - 73,524 \\ \hline \end{array}$
39. $\begin{array}{r} 400,000 \\ - 70,293 \\ \hline \end{array}$	40. $\begin{array}{r} 1030 \\ - 987 \\ \hline \end{array}$	41. $\begin{array}{r} 41,020 \\ - 9,382 \\ \hline \end{array}$	42. $\begin{array}{r} 310,015 \\ - 73,046 \\ \hline \end{array}$
43. $\begin{array}{r} 610,003 \\ - 685 \\ \hline \end{array}$	44. $\begin{array}{r} 100,000 \\ - 73,600 \\ \hline \end{array}$		

45. Carlos had \$50 in his pocket. He spent \$12 on lunch for himself and his friend Dorothy. How much money does he have left?

APPLICATION PROBLEMS

- There are 120 passengers on board an airplane. $\frac{2}{3}$ of them are men, $\frac{1}{4}$ are women and the rest are children. How many children are there?
- There are 350 members in a swimming club. $\frac{2}{7}$ of them are new members. $\frac{3}{10}$ of the new members are females. How many new female members are there?
- Sally made 500 cookies. She sold $\frac{3}{4}$ of them and gave away $\frac{2}{5}$ of the remainder. How many cookies did she give away?
- Dani made some sticks of satay for a party. $\frac{3}{5}$ of them were chicken satay and the rest were beef satay. There were 240 sticks of beef satay. How many sticks of chicken satay were there?
- After paying \$30 for a shirt, David had $\frac{3}{5}$ of his money left. How much money did he have at first?
- After spending $\frac{2}{5}$ of his money on a storybook, Mathew had \$12 left. How much did he spend on the storybook?



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(An attempt to find balance)

Looking at a **diverse population**.

A.
Simplify.

1. $5 \cdot 8 + 13$	17 + 5 · 6	3. $15 - 5 \cdot 3$
4. $28 \cdot 4 - 7$	5. $24 \div 2$	6. $36 \div 6 - 3$
7. $30 - (13 + 2)$	8. $(19 - 3) - 8$	9. $30 \div 6 \times 5$
10. $45 \div 5 \times 3$	11. $21 + 5 \cdot 4 - 2$	12. $25 - 3 \cdot 7 + 4$
13. $3^4 + 4^3$	14. $3^5 - 2^4 + 7^2$	

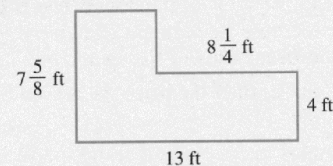
B.
Simplify.

15. $4 \cdot 7 + 3 \cdot 5$	16. $6 \cdot 7 - 5 \cdot 4$	17. $3^2 - 4 \cdot 2 + 5 \cdot 6$
18. $5^2 + 12 \div 3 + 3 \cdot 3$	19. $36 \div 9 + 8 - 5$	20. $56 \cdot 3 \div 14 + 4 - 6$
21. $(14 + 28) - (34 - 27)$	22. $(56 - 8) - (17 + 7)$	

DRILL and PRACTICE

Whether a student's native language is English or not, many adapt to drill and practice.

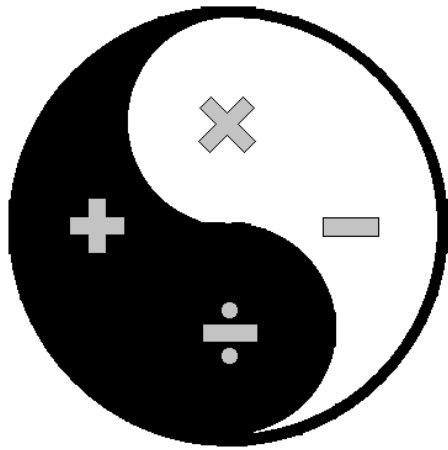
26. Five boxes weigh $7\frac{1}{2}$ pounds each and three boxes weigh $5\frac{2}{3}$ pounds each. What is the average weight of the 8 boxes?
27. Alice has \$500. She spends $\frac{2}{5}$ of it for clothes. How much money is left?
28. A math class has 56 students. Five-eighths of the class are men. How many women are in the class?
29. Sally saved \$150 out of a monthly income of \$2400. Mary saved \$125 out of a monthly income of \$1500. Which person saved the larger fractional portion of her income, and what is the difference in these fractions?
30. A stock decreased in price from \$30 to $\$28\frac{3}{4}$. The decrease in price is what fraction of the original price?
31. Find the perimeter around this floor space.



32. Find the total area of this region.

APPLICATIONS and READING

For students whose language is **NOT** English, it is another hurdle. Native born students also have difficulty.



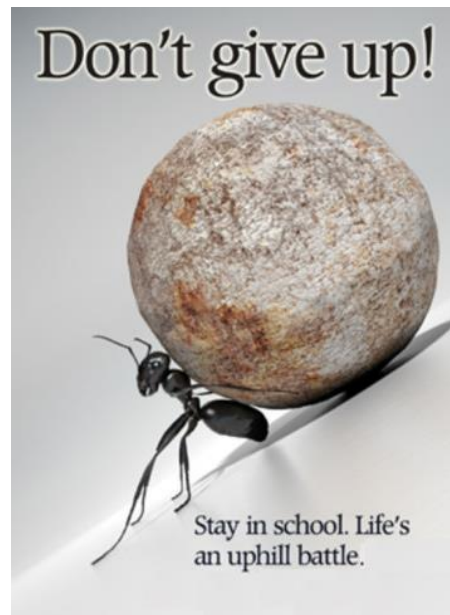
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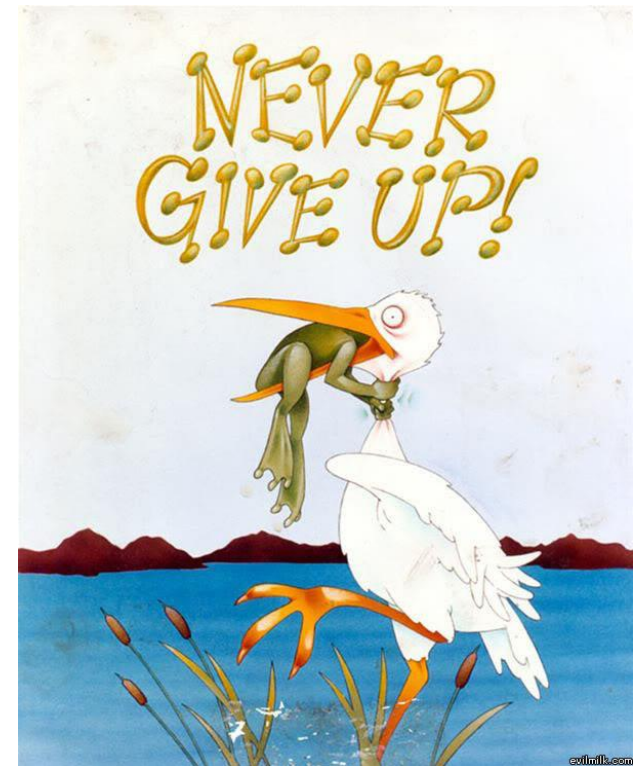
Looking at **PERSISTENCE**



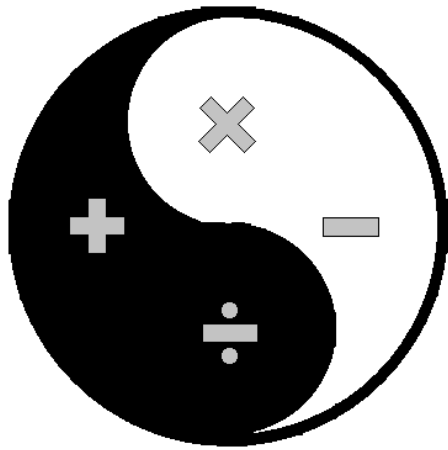
MATH ANXIETY
(w/excuse)



ENCOURAGEMENT
(Find a bone for the dog)

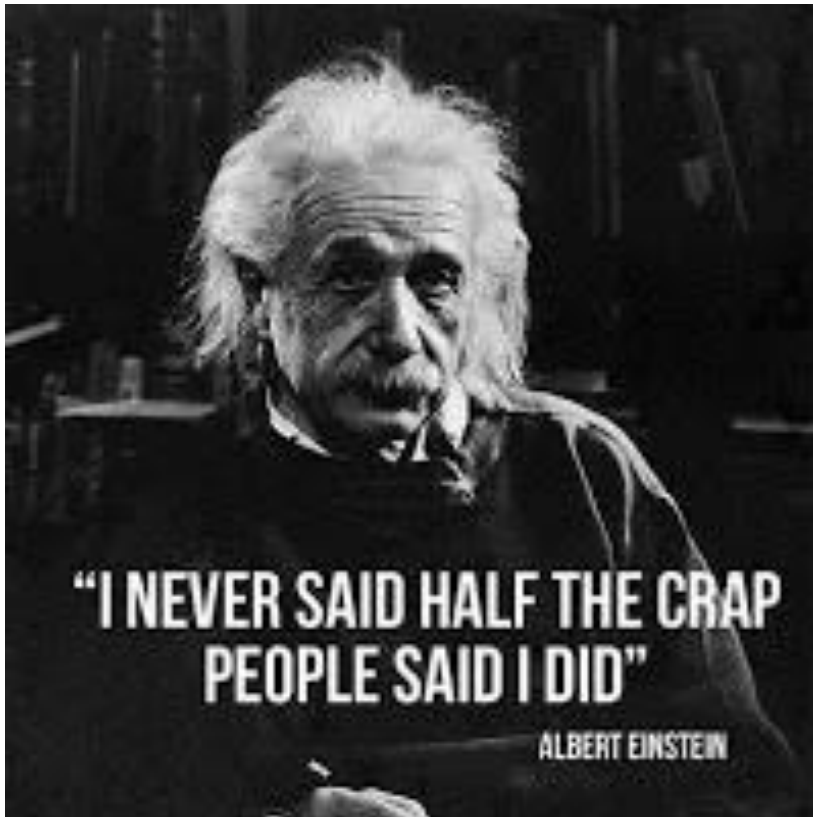


HOPEFUL RESULT 
(Found a bone for the dog)

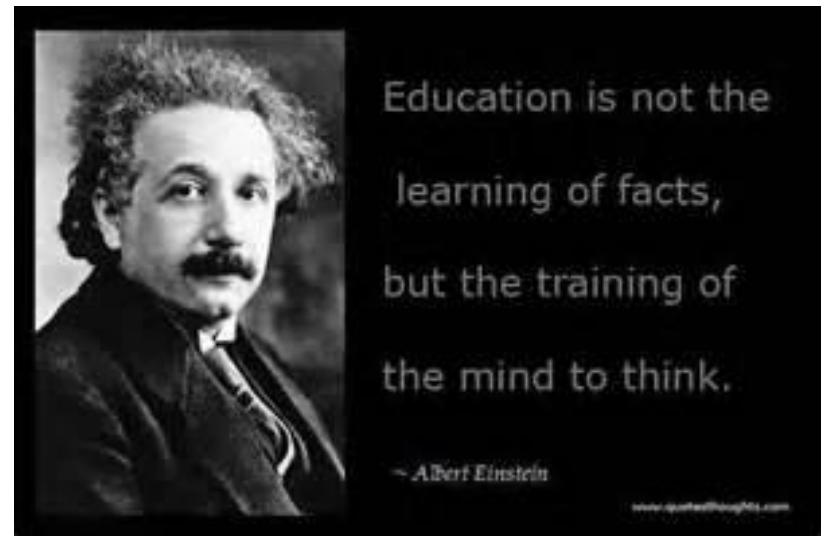


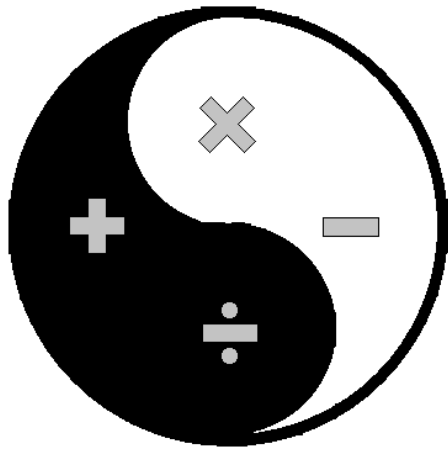
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In most cases, there should not be a difference in what we say and what we do. I looked to Albert Einstein for his experience and intellect for what I should be **teaching** in my classroom. It is still a matter of choice, and I choose to believe the statement below.





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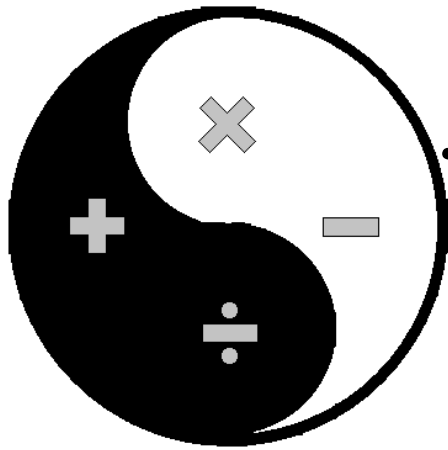
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*In dealing with **PROBLEM SOLVING**, one has three areas to address.*



- Create an environment for learning
- Promote discovery and long-term understanding
- Support and Encourage Persistence

Anxiety	Feelings Continuum	Confidence	Psychological/ Emotional
Failure	Achievement Continuum	Success	Intellectual/ Educational
Avoidance	Behavioral Continuum	Pursuit	Social/ Motivational



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Creating an Environment for



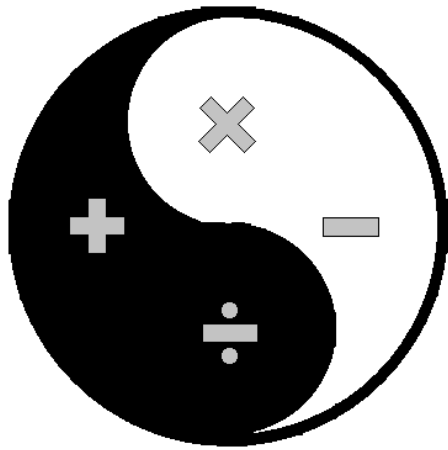
Create an environment
for learning

Anxiety



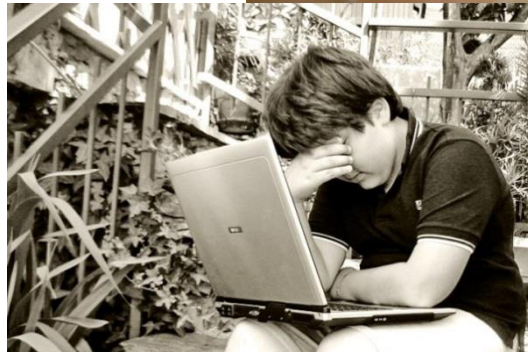
Confidence

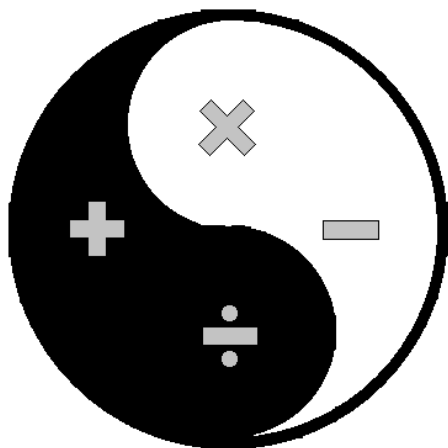
Psychological/
Emotional



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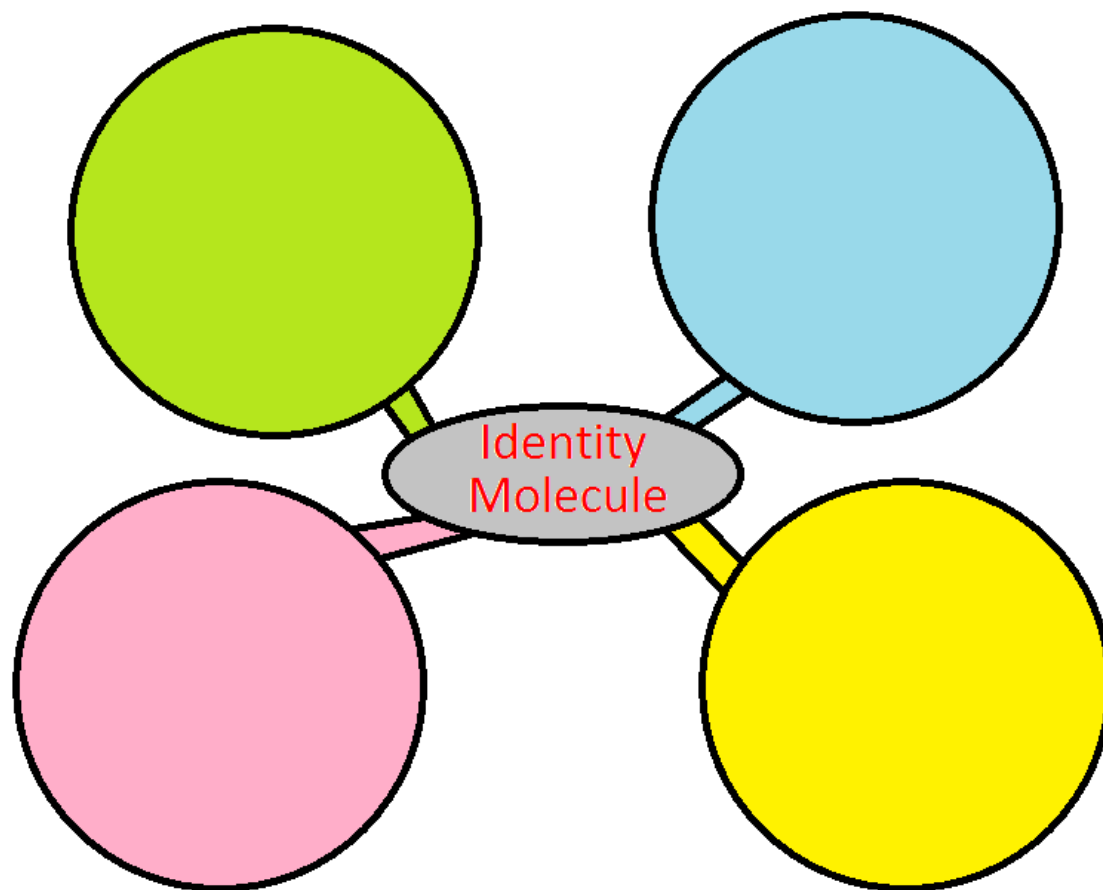


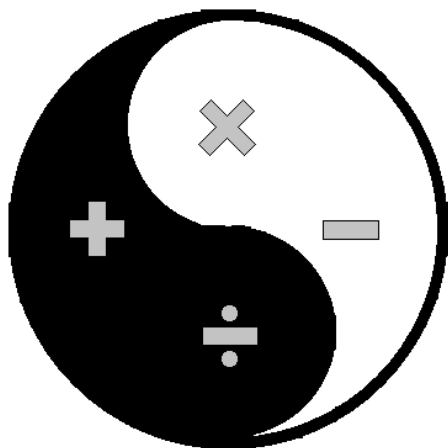
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Addressing Isolation

In each circle, write something that is **important** to you, and perhaps, you would like others to know about you.



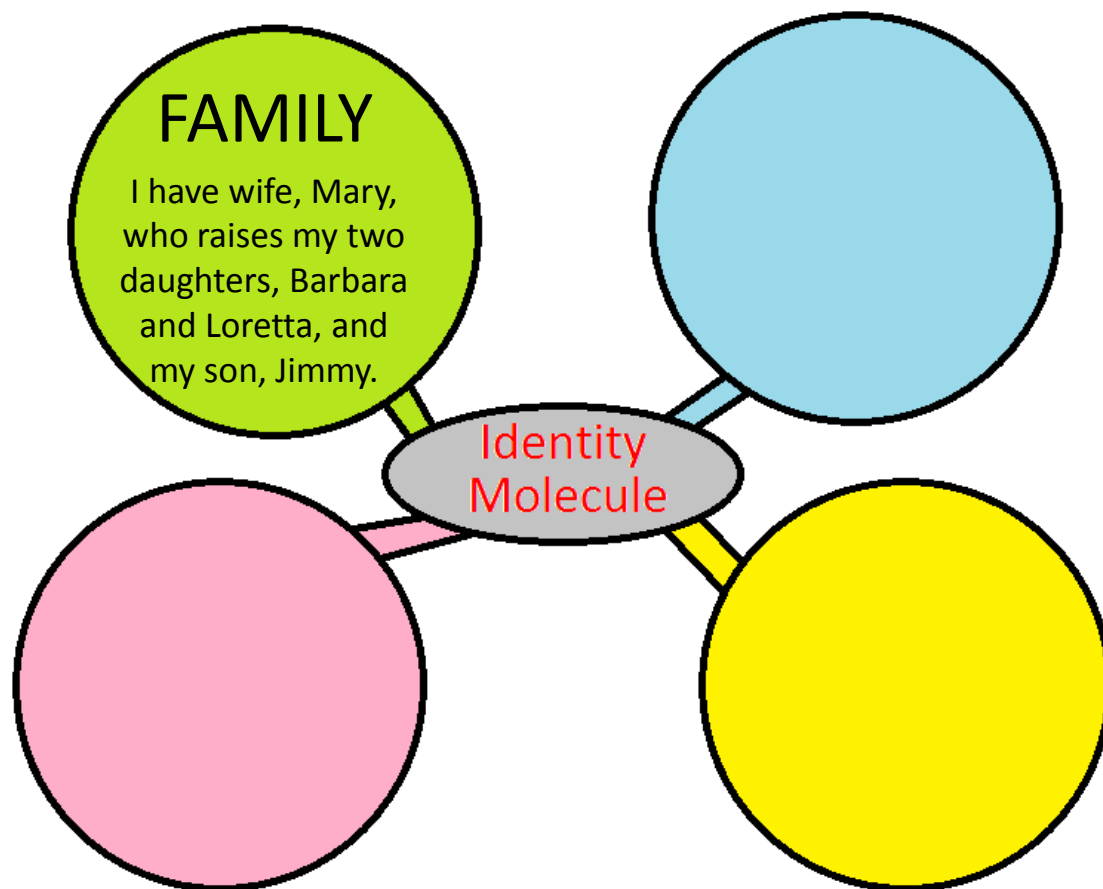


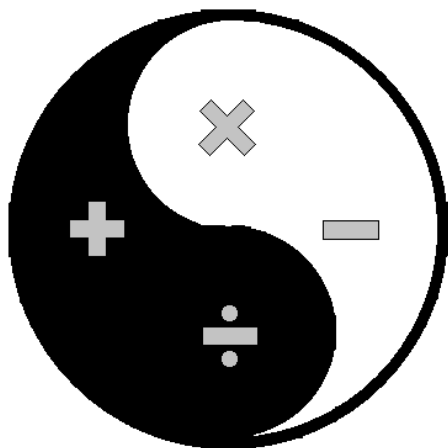
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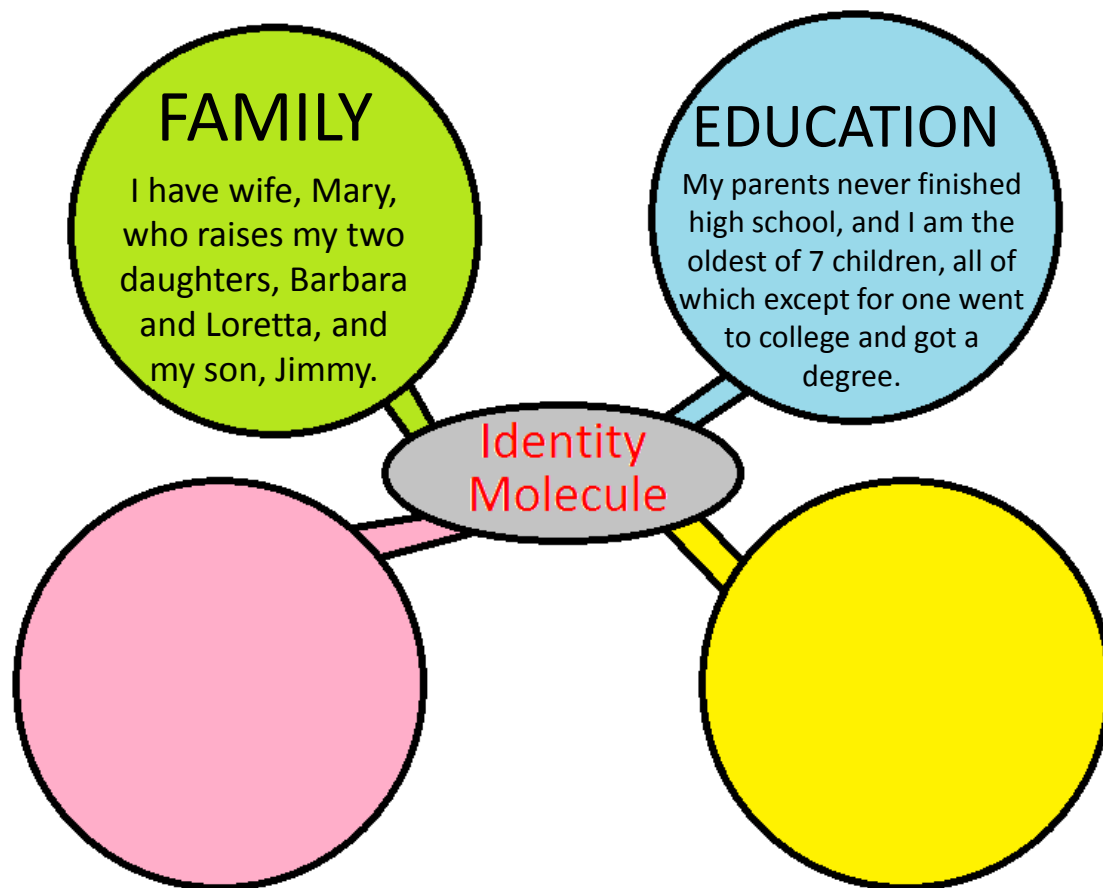


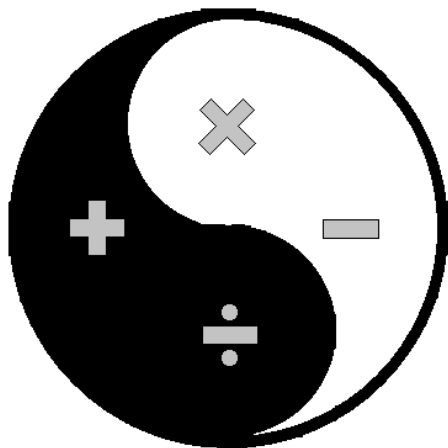
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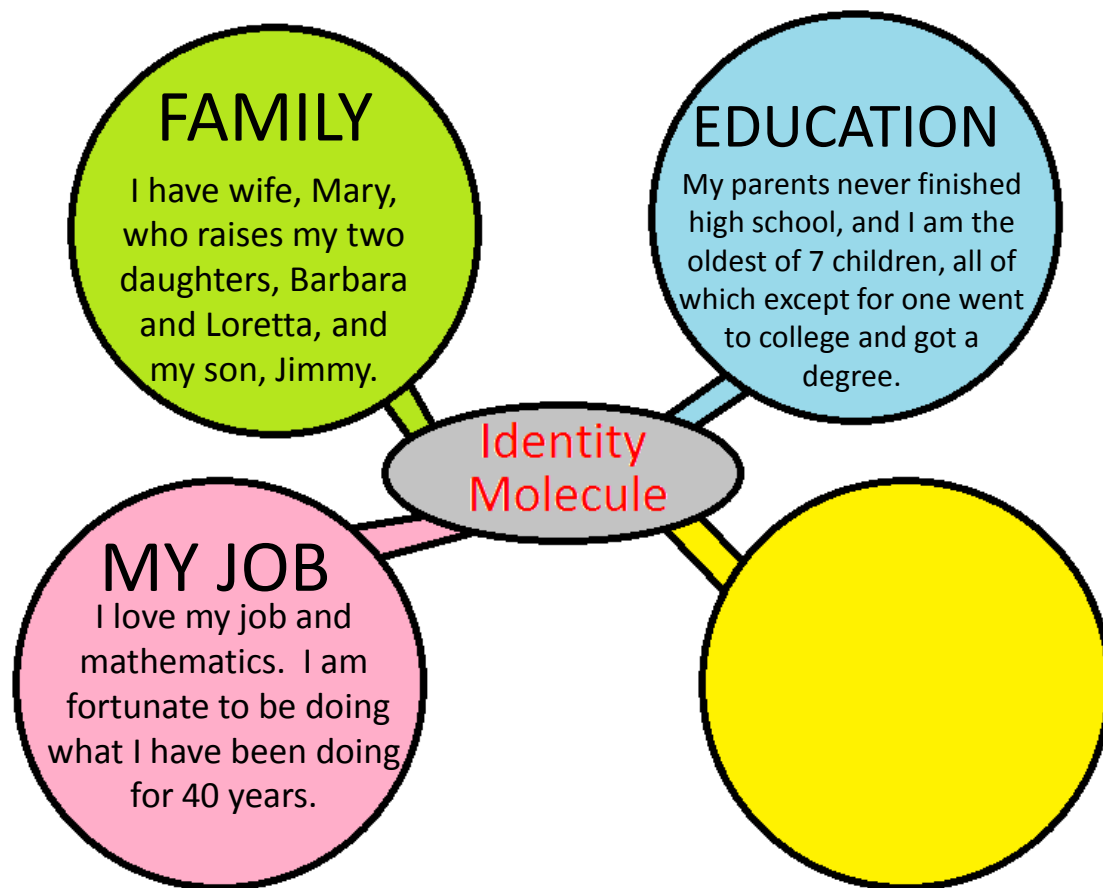


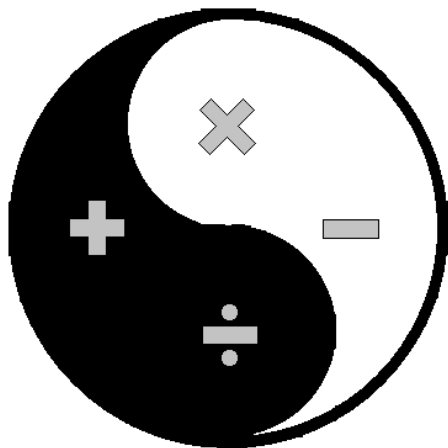
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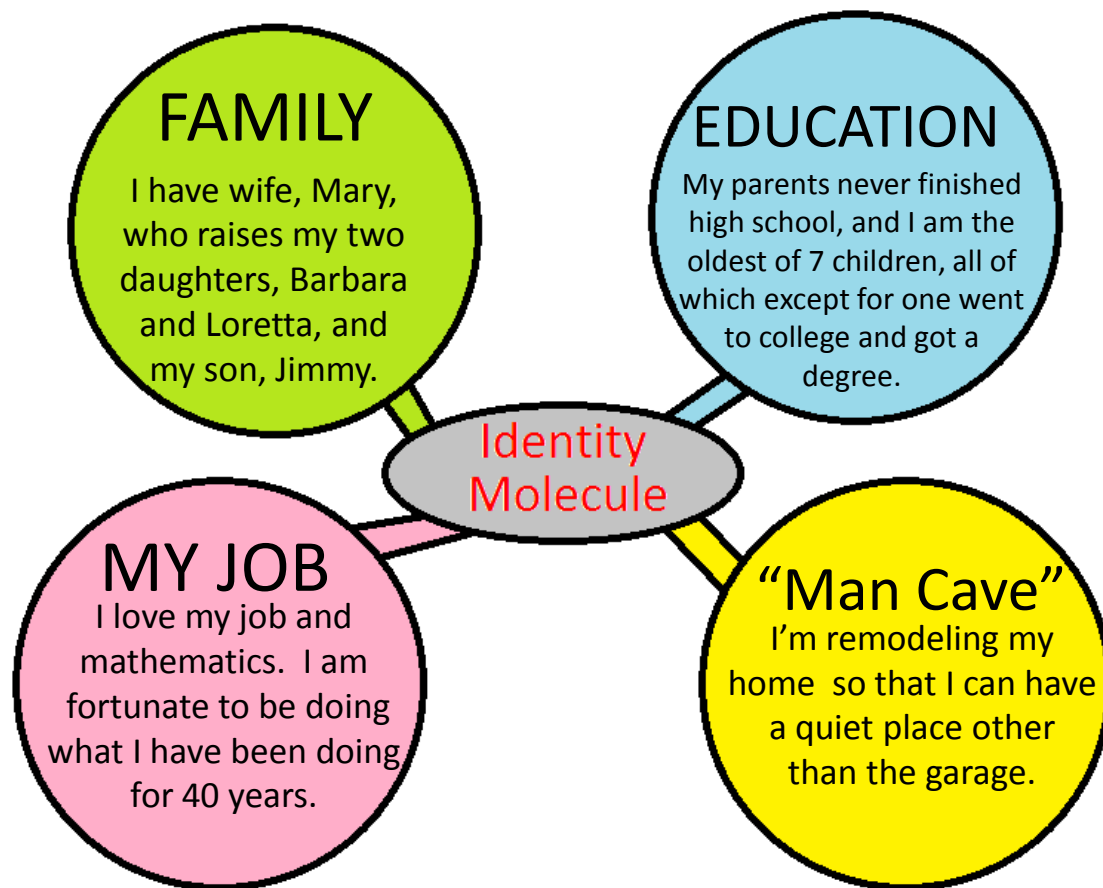


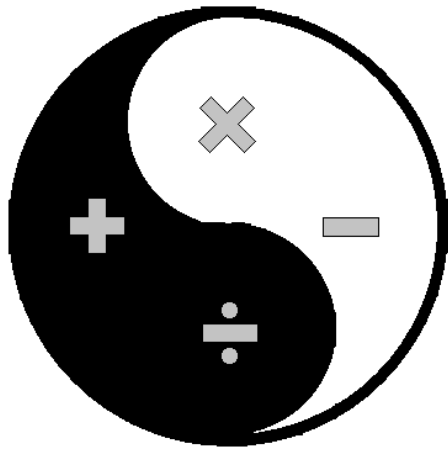
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Promote Discovery and Long-term Understanding

Yin Cycle



Yang Cycle

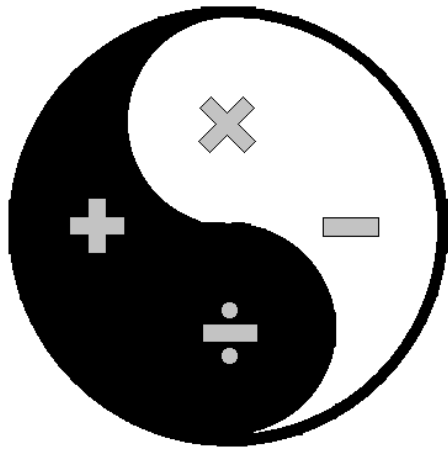
Promote discovery and long-term understanding

Failure



Success

Intellectual/
Educational



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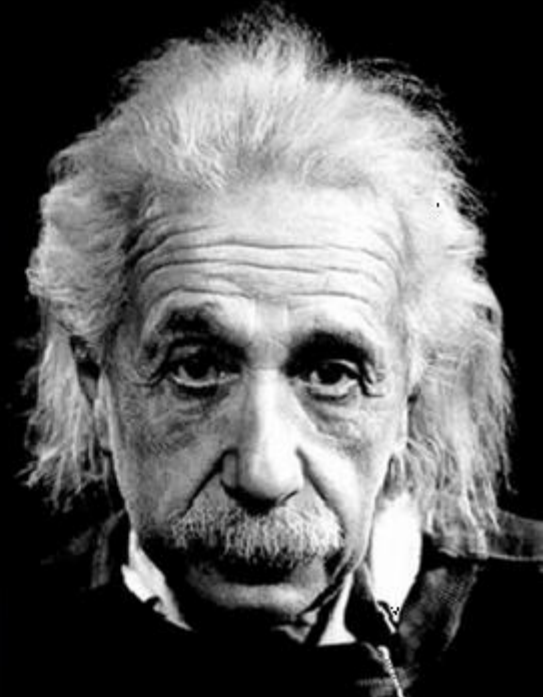
“Challenge the Familiar”

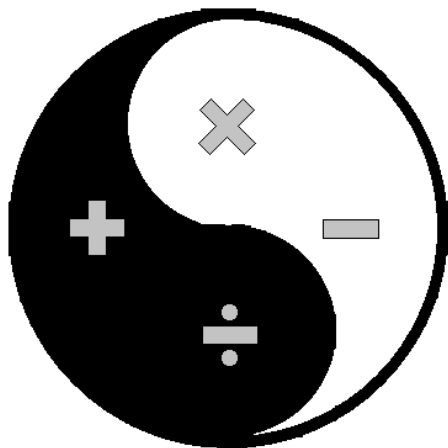
Model mathematics
and let their innate
skills develop.

9			
2			

“Everything should be made
as simple as possible,
but not simpler.”

Albert Einstein



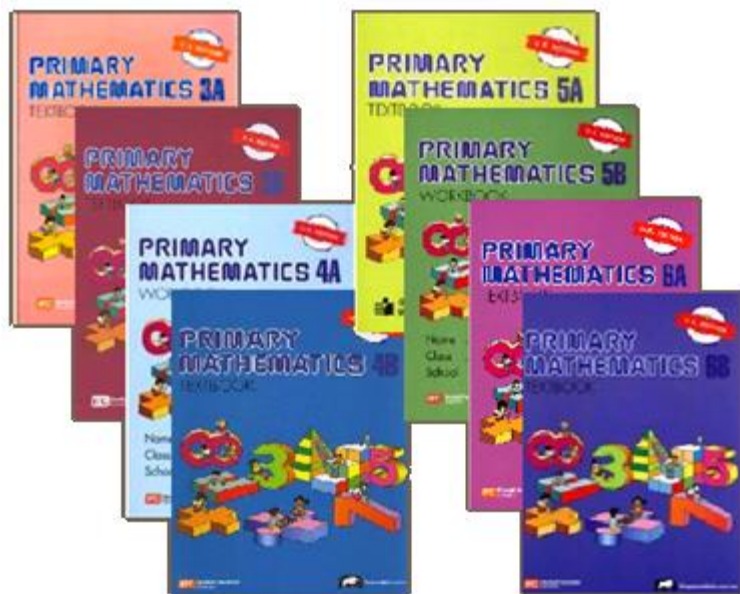


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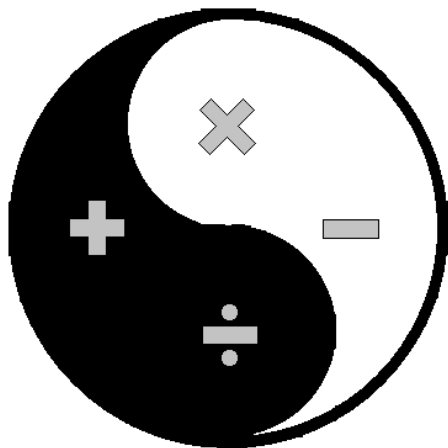
“AND Embrace the Unfamiliar”



		5
3		
6		

What is the initial value of the shaded region?

A primary component of the Singapore Math course is the use of visual representations of mathematical quantities and its role in problem solving single and multi-step applications.



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"Extend to the Familiar"

Evaluating the expression when $x = 9$

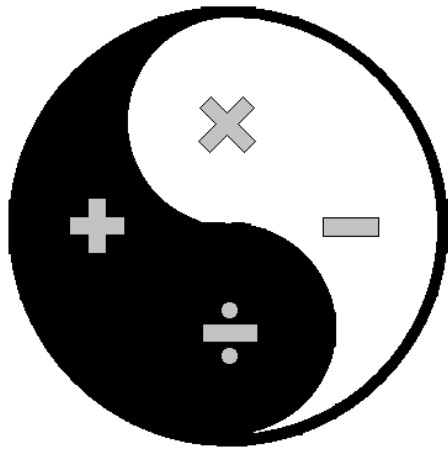
$$\frac{3}{5} (3x - 2).$$

9				
2				

Solving the equation $\frac{2x+5}{3} - 3 = 6.$

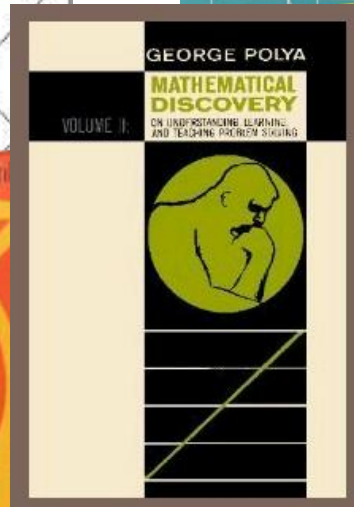
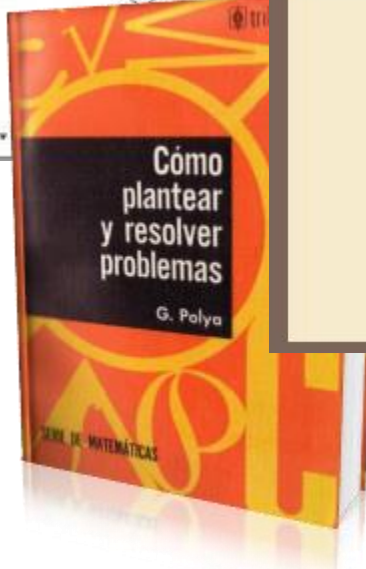
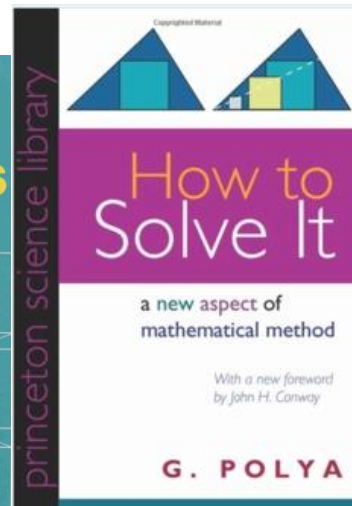
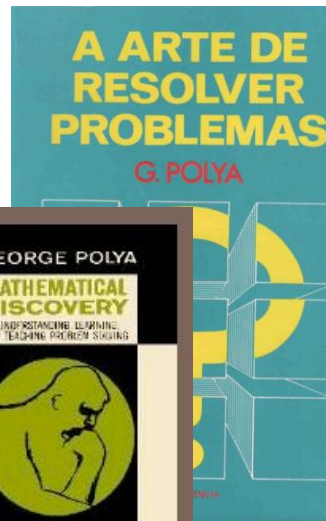
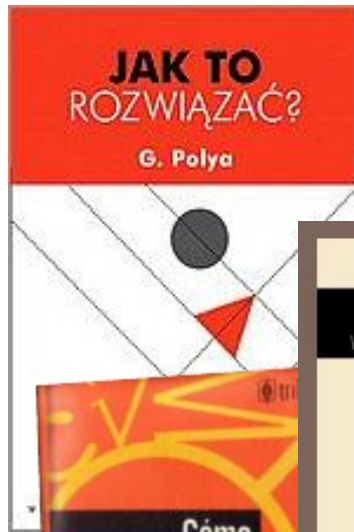
		5
3		
	6	

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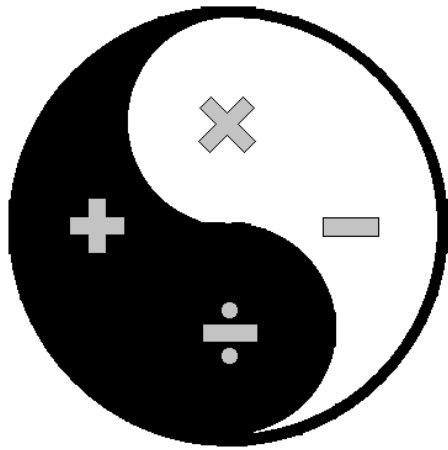


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PROBLEM SOLVING
STARTS WITH BASIC
MATHEMATICS



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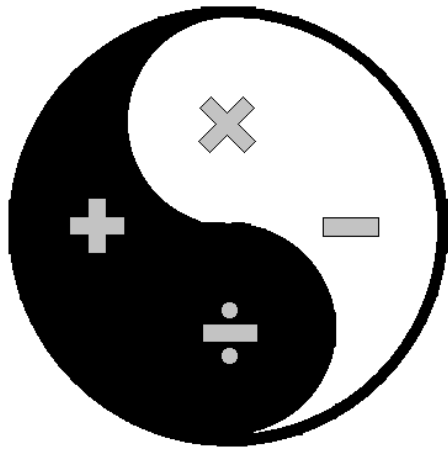
1. Understand the problem

Paul and Cheryl are selling hats. Cheryl purchased **two boxes** of hats while Paul purchased **three times as many**. If **$\frac{5}{6}$ of Paul's purchase is 10** hats, how many hats did each of them purchase?

2. Devise a plan

3. Carry out the plan

4. Look back



The Tai Chi of Basic Mathematics

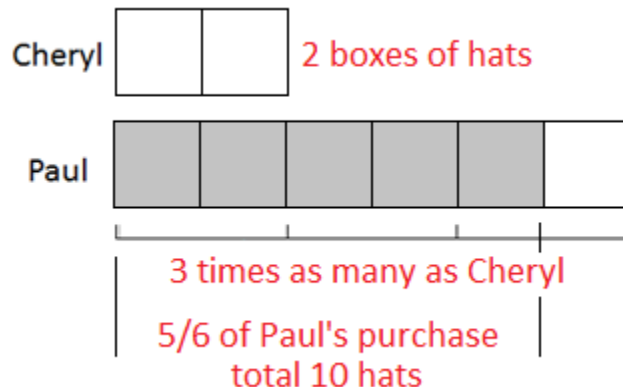
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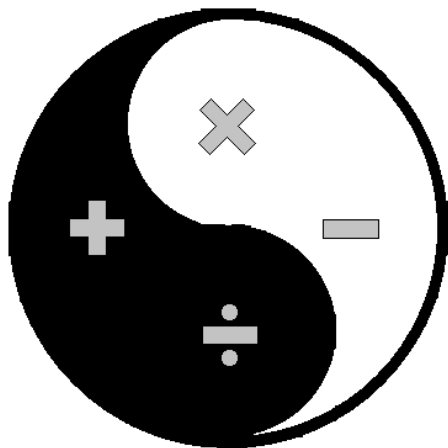
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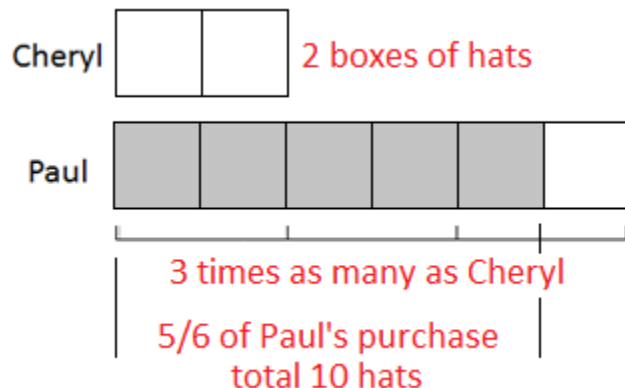
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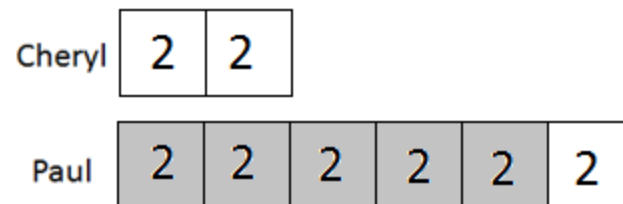
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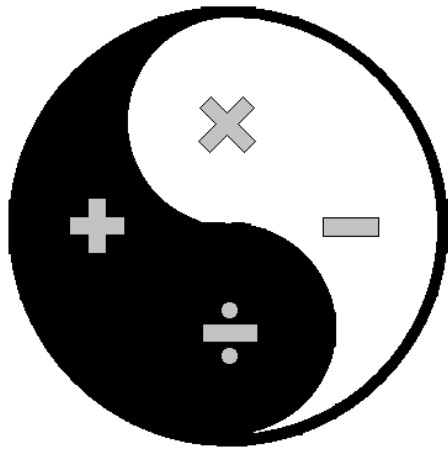
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4. Look back



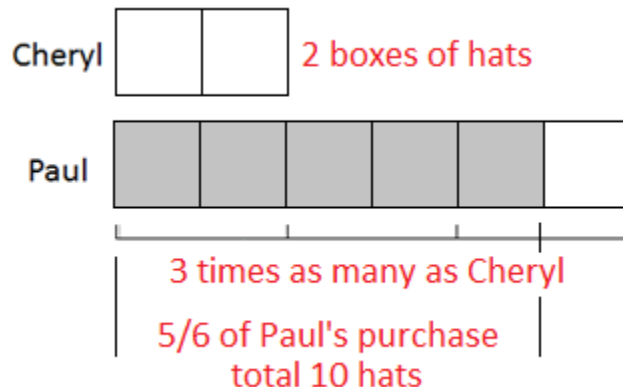
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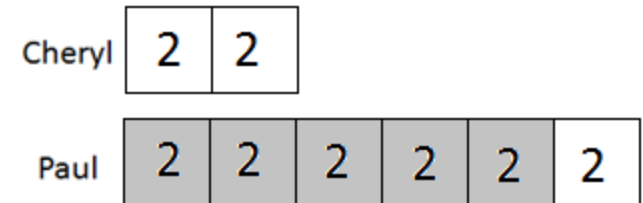
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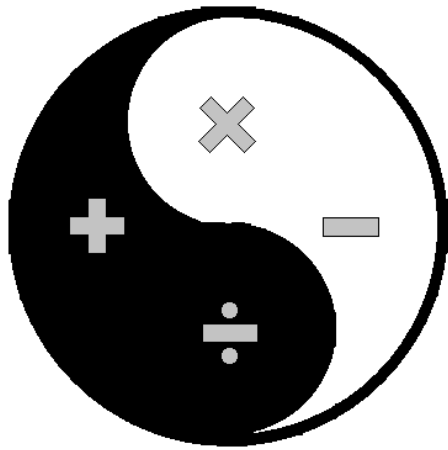
Cheryl bought **4 hats** and Paul purchased **12 hats**.

$\frac{5}{6}$ of 12 is 10.



Given the information below, what is the value of the shaded regions.

83		
37		
17		



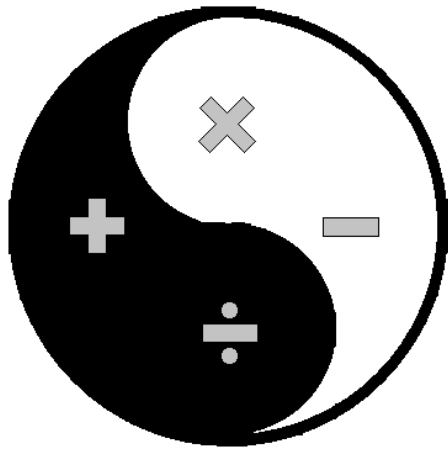
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PROBLEM SOLVING (Words → Models → Solutions)

Fred could not **divide** the amount of money in his pocket equally among his 4 kids. His wife gave him an **additional** \$3 after which each of his 4 kids received \$8.



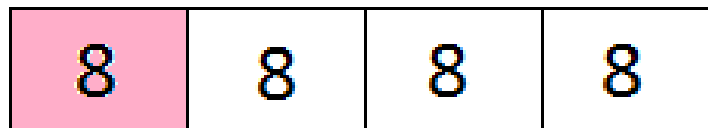


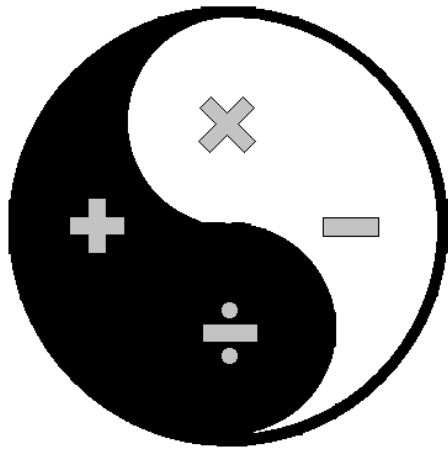
The Tai Chi of Basic Mathematics

(An attempt to find balance)

PROBLEM SOLVING (Words → Models → Solutions)

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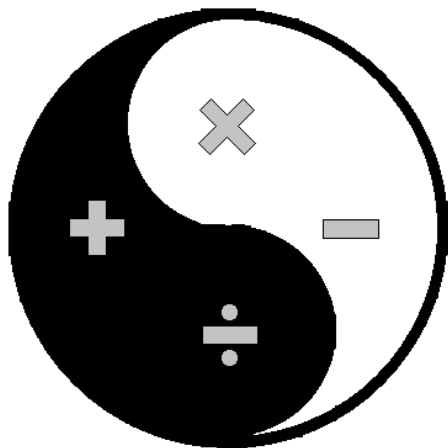
The Tai Chi of Basic Mathematics

(An attempt to find balance)

PROBLEM SOLVING (Words → Models → Solutions)

Tristan **divided** a certain amount of money **into 3 equal shares**. He gave the first share to Betty, the second share to Veronica, and he then **divided the remainder** into 3 equal shares and gave one share to Archie. He kept the rest totaling \$24. How much money did Tristan **initially** have?



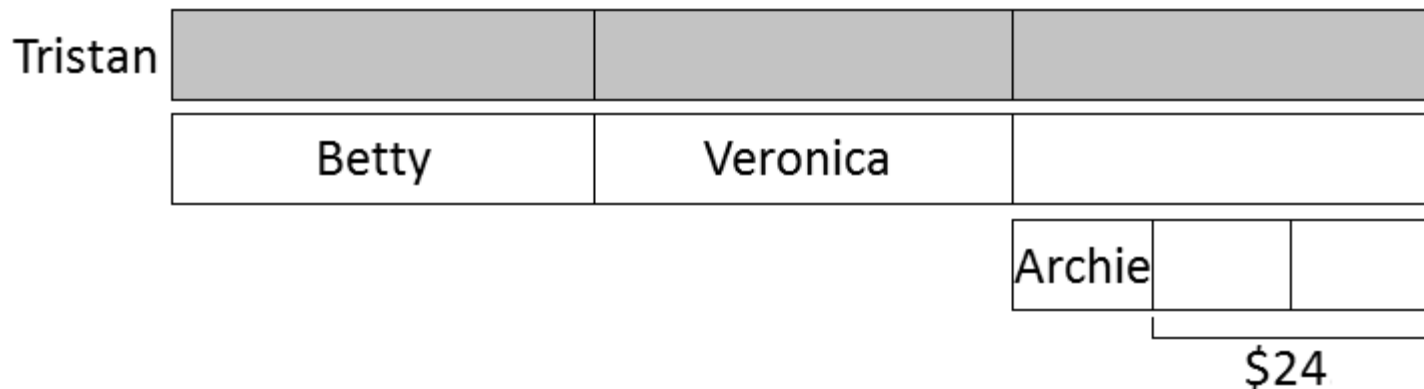


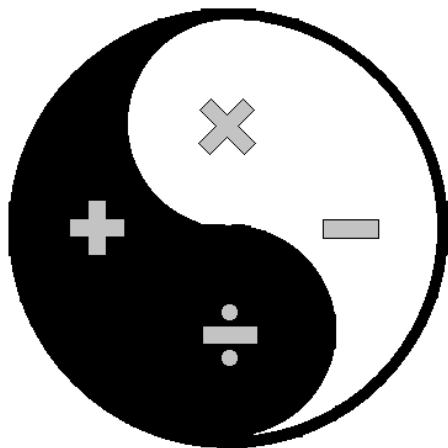
The Tai Chi of Basic Mathematics

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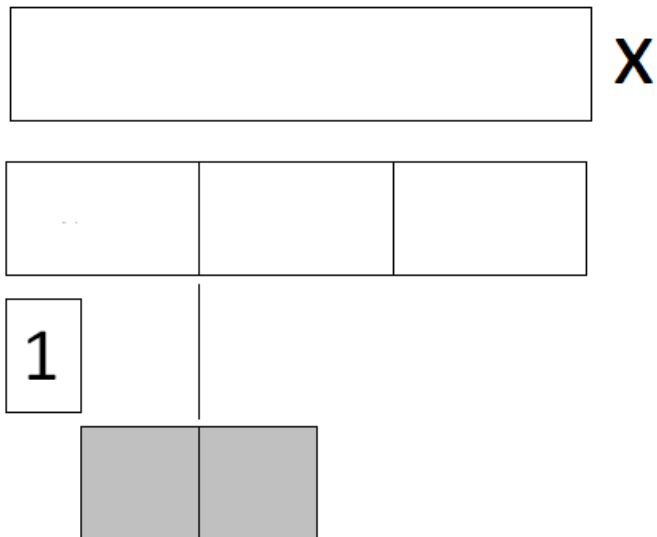
The Tai Chi of Basic Mathematics

(An attempt to find balance)

PROBLEM SOLVING and Linear Models → Expression

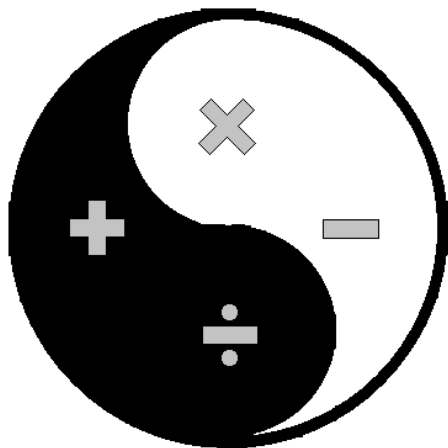
Given the model, create the algebraic expression.

Illustration:



What is the
Algebraic Expression?





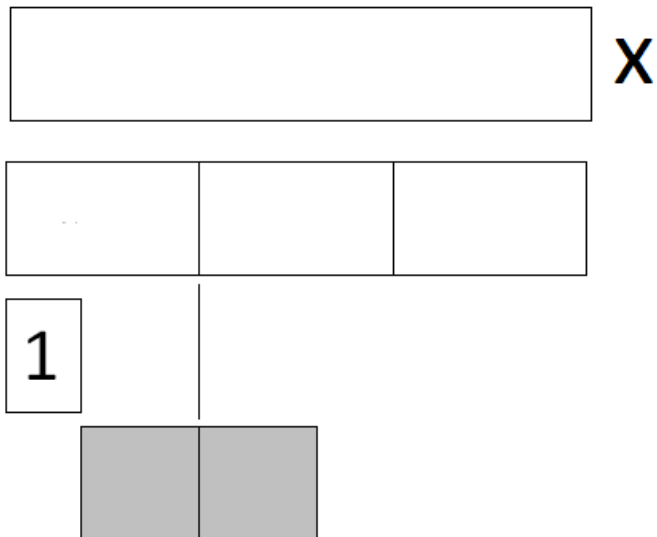
The Tai Chi of Basic Mathematics

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PROBLEM SOLVING and Linear Models → Expression

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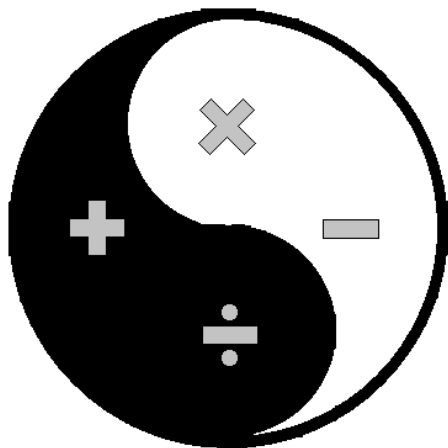
Illustration:



What is the Algebraic Expression?

$$2\left(\frac{x}{3} - 1\right)$$





The Tai Chi of Basic Mathematics

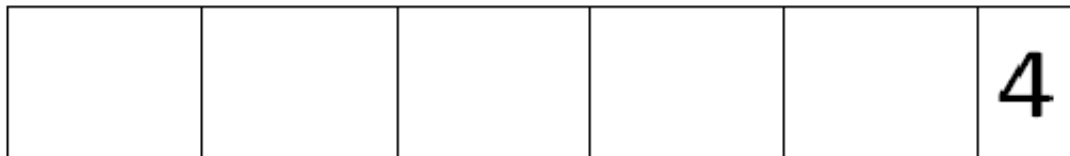
(An attempt to find balance)

PROBLEM SOLVING and Linear Models → Expression

Given the model, create the algebraic expression.

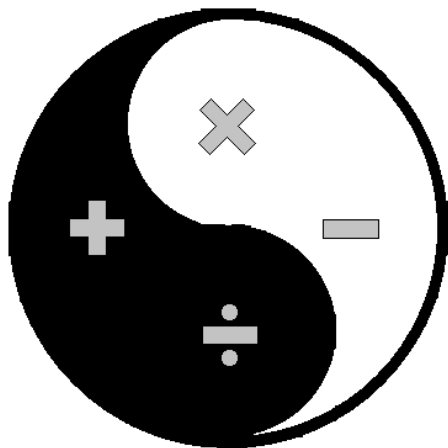


Illustration:



What is the Algebraic Expression?





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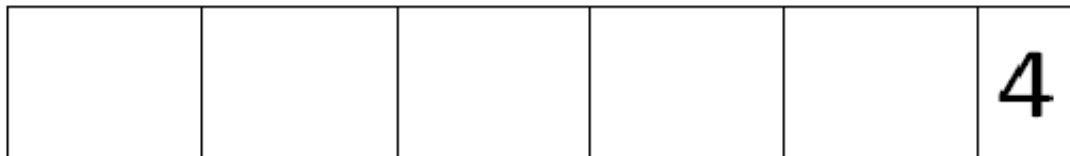
(An attempt to find balance)

PROBLEM SOLVING and Linear Models → Expression

Given the model, create the algebraic expression.



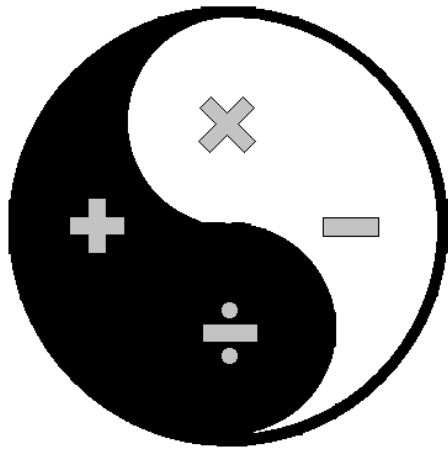
Illustration:



What is the Algebraic Expression?

$$\frac{2}{3}(5x + 4)$$





The Tai Chi of Basic Mathematics

(An attempt to find balance)

Linear Functions and the Order of Operations → Model

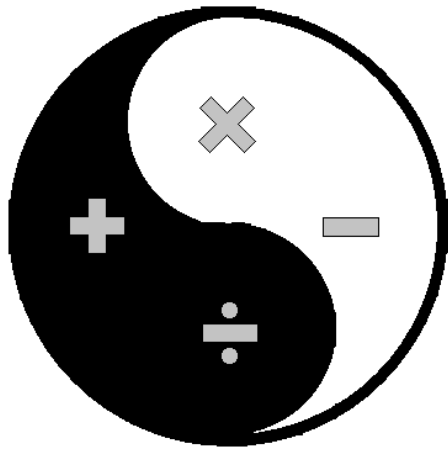
Given the algebraic expression, label the order of each operation involve in the process, and then create the model.

X

$$3\left(\frac{X}{2} + 5\right)$$

3 Operations





The Tai Chi of Basic Mathematics

(An attempt to find balance)

Linear Functions and the Order of Operations → Model

Given the algebraic expression, label the order of each operation involve in the process, and then create the model.

Op 1 **DIVISION**

X

$$3\left(\frac{x}{2} + 5\right)$$

3 Operations





Given the algebraic expression, label the order of each operation involve in the process, and then create the model.

X

--	--

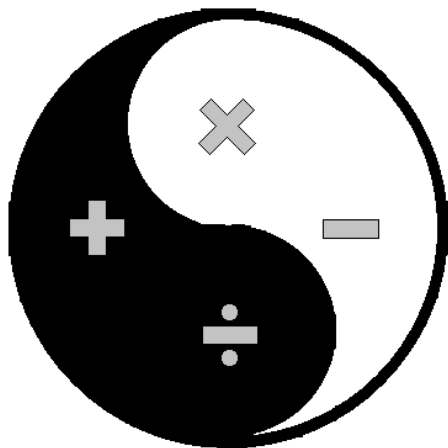
Diagram illustrating the distributive property of multiplication over addition:

$$3\left(\frac{x}{2} + 5\right)$$

The diagram shows the expression $3\left(\frac{x}{2} + 5\right)$ with arrows indicating the distribution of the factor 3 to each term inside the parentheses:

- Arrow 1 points from the 3 to $\frac{x}{2}$.
- Arrow 2 points from the 3 to 5.





The Tai Chi of Basic Mathematics

(An attempt to find balance)

Linear Functions and the Order of Operations → Model

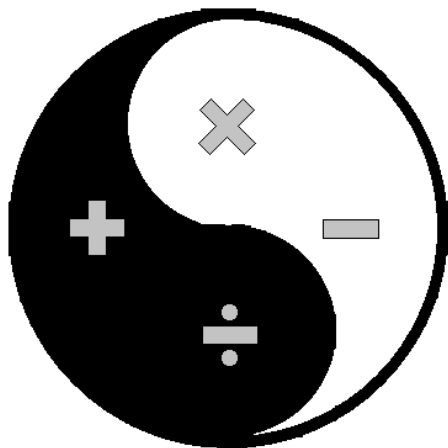
Given the algebraic expression, label the order of each operation involve in the process, and then create the model.

	<div style="border: 1px solid black; width: 300px; height: 40px;"></div>	x
Op 1 DIVISION	<div style="display: inline-block; width: 150px; height: 40px; background-color: yellow; border: 1px solid black;"></div> <div style="display: inline-block; width: 150px; height: 40px; border: 1px solid black;"></div>	
Op 2 SUM	<div style="display: inline-block; width: 150px; height: 40px; border: 1px solid black;"></div> <div style="display: inline-block; width: 30px; height: 40px; border: 1px solid black; text-align: center; vertical-align: middle;">5</div>	
Op 3 TIMES	<div style="display: inline-block; width: 180px; height: 40px; background-color: #cccccc; border: 1px solid black;"></div> <div style="display: inline-block; width: 180px; height: 40px; background-color: #cccccc; border: 1px solid black;"></div> <div style="display: inline-block; width: 180px; height: 40px; background-color: #cccccc; border: 1px solid black;"></div>	

$$3\left(\frac{x}{2} + 5\right)$$

3 Operations





The Tai Chi of Basic Mathematics

(An attempt to find balance)

Linear Functions and the Order of Operations → Model

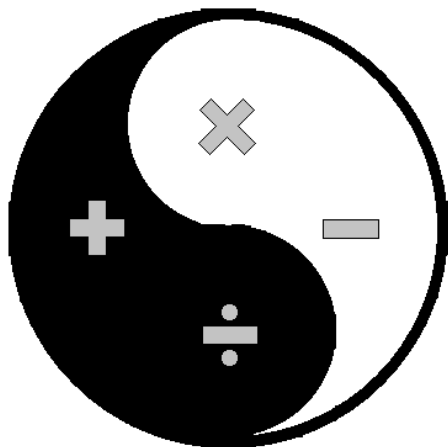
Given the algebraic expression, label the order of each operation involve in the process, and then create the model.

x

$$\begin{array}{c} 1 \swarrow \quad \quad \quad \nearrow 2 \quad \quad \quad \nearrow 4 \\ 3\left(\frac{x}{4} + 1\right) + 2 \\ \swarrow 3 \quad \quad \quad \searrow 5 \\ \hline 5 \end{array}$$

5 Operations





The Tai Chi of Basic Mathematics

(An attempt to find balance)

Linear Functions and the Order of Operations → Model

Given the algebraic expression, label the order of each operation involve in the process, and then create the model.

Op 1 **DIVIDE**

				X

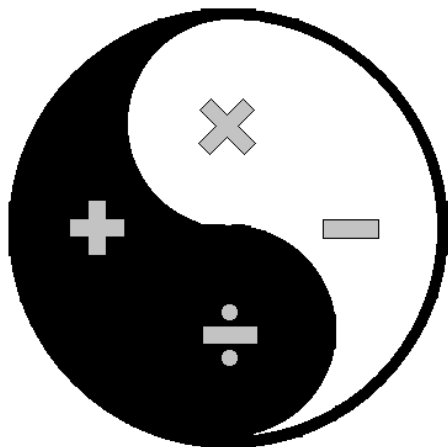
$$3\left(\frac{x}{4} + 1\right) + 2$$

Diagram illustrating the order of operations for the expression $3\left(\frac{x}{4} + 1\right) + 2$:

- 1: Division ($\frac{x}{4}$)
- 2: Addition ($\frac{x}{4} + 1$)
- 3: Multiplication ($3 \times (\frac{x}{4} + 1)$)
- 4: Addition ($3(\frac{x}{4} + 1) + 2$)
- 5: Final result (5)

5 Operations





The Tai Chi of Basic Mathematics

(An attempt to find balance)

Linear Functions and the Order of Operations → Model

Given the algebraic expression, label the order of each operation involve in the process, and then create the model.

Op 1 **DIVIDE**

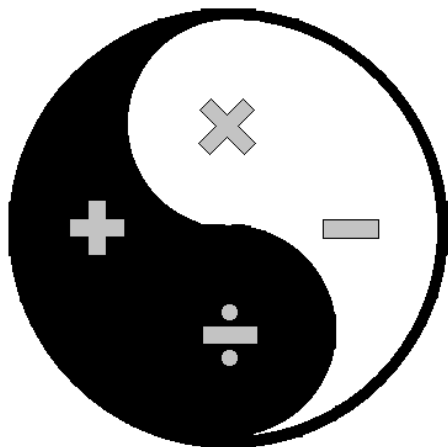
Op 2 **SUM**

				x
		1		

$$\begin{array}{c}
 \begin{array}{ccccc}
 & 1 & & 2 & & 4 \\
 & \swarrow & & \swarrow & & \swarrow \\
 3 & \left(\frac{x}{4} + 1 \right) + 2 \\
 \hline
 3 & & & & & 5 \\
 & \searrow & & \searrow & & \\
 & 5 & & & &
 \end{array}
 \end{array}$$

5 Operations





The Tai Chi of Basic Mathematics

(An attempt to find balance)

Linear Functions and the Order of Operations → Model

Given the algebraic expression, label the order of each operation involve in the process, and then create the model.

Op 1 **DIVIDE**

--	--	--	--

X

Op 2 **SUM**

--	--	--	--

Op 3 **TIMES**

	1
--	---

--	--	--

$$3\left(\frac{X}{4} + 1\right) + 2$$

Diagram illustrating the order of operations for the expression $3\left(\frac{X}{4} + 1\right) + 2$:

- 1: Division ($X/4$)
- 2: Addition ($+ 1$)
- 3: Multiplication ($3 \times$)
- 4: Addition ($+ 2$)
- 5: Final result (5)

5 Operations





Linear Functions and the Order of Operations → Model

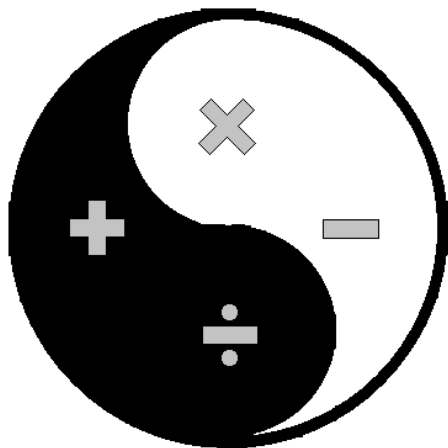
Op 1 **DIVIDE**

Op 2 SUM

Op 3 **TIMES**

Op 4 SUM
$$3\left(\frac{x}{4} + 1\right) + 2$$

$$5$$

The Tai Chi of Basic Mathematics

(An attempt to find balance)

Linear Functions and the Order of Operations → Model

Given the algebraic expression, label the order of each operation involve in the process, and then create the model.

					X
Op 1 DIVIDE					
Op 2 SUM		1			
Op 3 TIMES					
Op 4 SUM				2	
Op 5 DIVIDE					

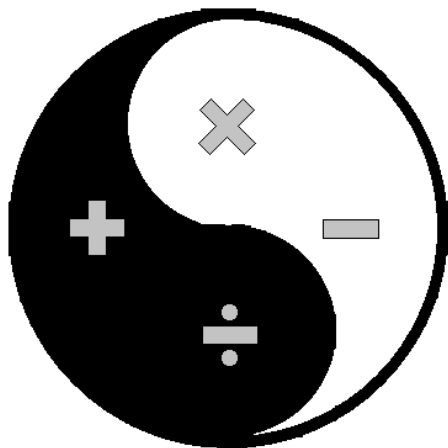
$$3\left(\frac{X}{4} + 1\right) + 2$$

Diagram illustrating the order of operations for the expression $3\left(\frac{X}{4} + 1\right) + 2$:

- 1: Division ($X/4$)
- 2: Addition ($+ 1$)
- 3: Multiplication ($3 \times$)
- 4: Addition ($+ 2$)
- 5: Final result (5)

5 Operations





The Tai Chi of Basic Mathematics

(An attempt to find balance)

PROBLEM SOLVING: Evaluating an Expression.

Given the model and the corresponding input value, determine the value the expression.

90 \times

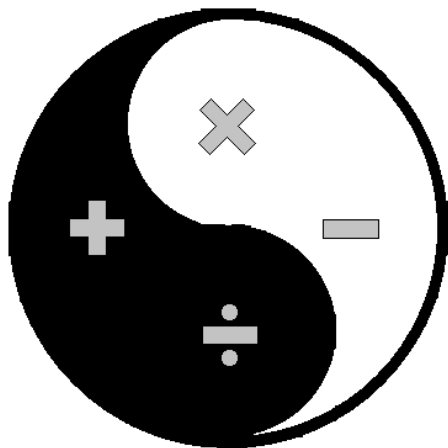
30

30 30 30 30 30 150

If the value of the x is 90, determine the value of the expression.

$$\frac{5}{3}x$$





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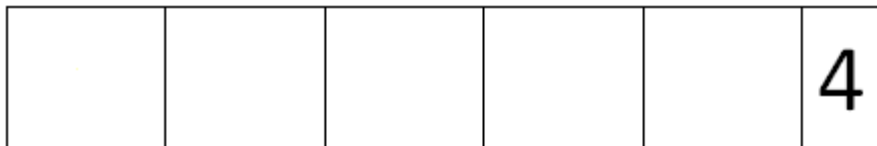
(An attempt to find balance)

PROBLEM SOLVING: Evaluating an Expression.

Given the model and the corresponding input value, determine the value the expression.

$$\boxed{7} \times$$

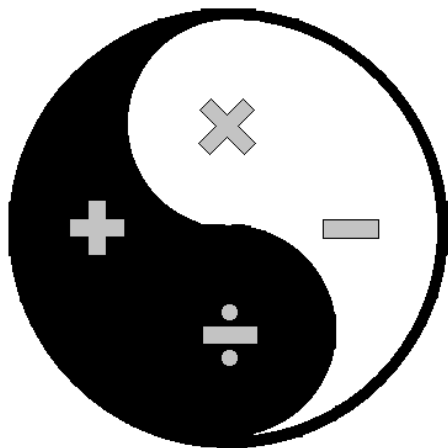
Illustration:



If the value of the x is 7, determine the value of the expression.

$$\frac{2}{3}(5x + 4)$$





The Tai Chi of Basic Mathematics

(An attempt to find balance)

PROBLEM SOLVING: Evaluating an Expression.

Given the model and the corresponding input value, determine the value the expression.

$$\boxed{7} \times$$

Illustration:

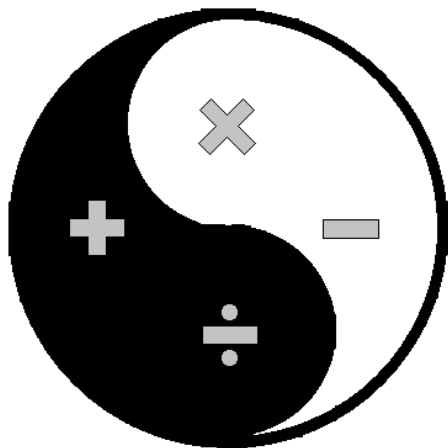
7	7	7	7	7	4	39
---	---	---	---	---	---	----

13	13	
----	----	--

If the value of the x is 7, determine the value of the expression.

$$\frac{2}{3}(5x + 4)$$





The Tai Chi of Basic Mathematics

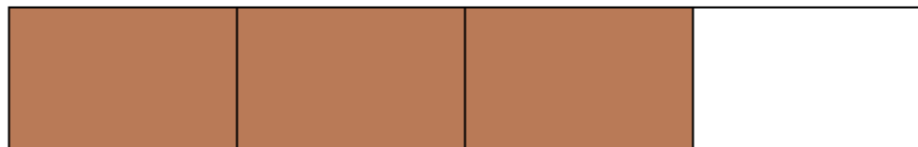
(An attempt to find balance)

PROBLEM SOLVING Models → Solving an Equation

Given the model and value of the expression, determine the value of its input.

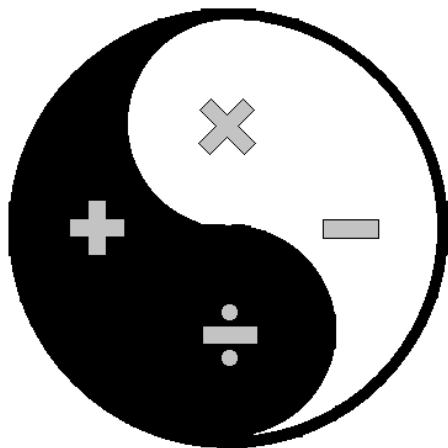


The expression has a value of 25; so what is the value of x ?



$$\left(\frac{3}{4}x + 4\right) = 25$$





The Tai Chi of Basic Mathematics

(An attempt to find balance)

PROBLEM SOLVING Models → Solving an Equation

Given the model and value of the expression, determine the value of its input.

28

X

The expression has a value of 25; so what is the value of x?

7

7

7

7

7

7

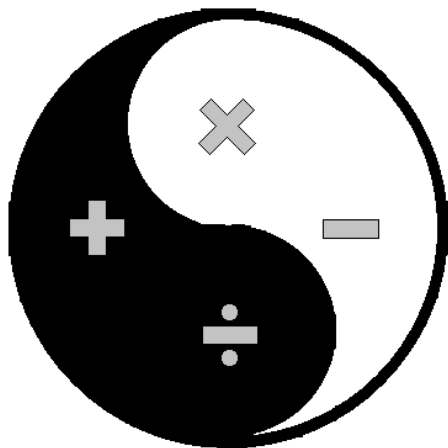
7

4

25

$$\left(\frac{3}{4}x + 4\right) = 25$$





The Tai Chi of Basic Mathematics

(An attempt to find balance)

PROBLEM SOLVING Models → Solving an Equation

Given the model and value of the expression, determine the value of its input.

Illustration:

--

x

The expression has a value of 8; so what is the value of x?

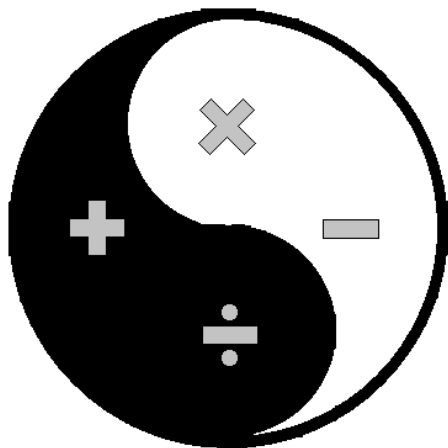
--	--	--	--	--	--	--	--	--	--

3	
	difference

4	4	
---	---	--

$$\frac{2}{3} \left(\frac{5}{9}x - 3 \right) = 8$$





The Tai Chi of Basic Mathematics

(An attempt to find balance)

PROBLEM SOLVING Models → Solving an Equation

Given the model and value of the expression, determine the value of its input.

Illustration:

x

The expression has a value of 8; so what is the value of x?

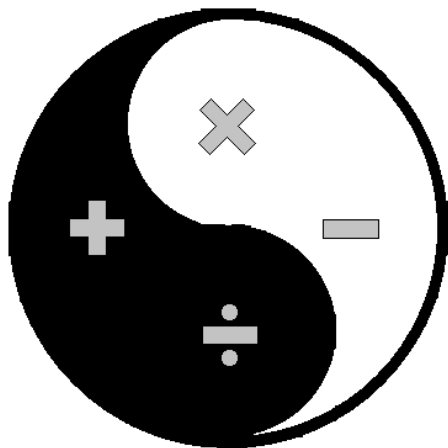
--	--	--	--	--	--	--	--	--	--

3	
	difference

4	4	4
---	---	---

$$\frac{2}{3} \left(\frac{5}{9}x - 3 \right) = 8$$





The Tai Chi of Basic Mathematics

(An attempt to find balance)

PROBLEM SOLVING Models → Solving an Equation

Given the model and value of the expression, determine the value of its input.

Illustration:

x

The expression has a value of 8; so what is the value of x?

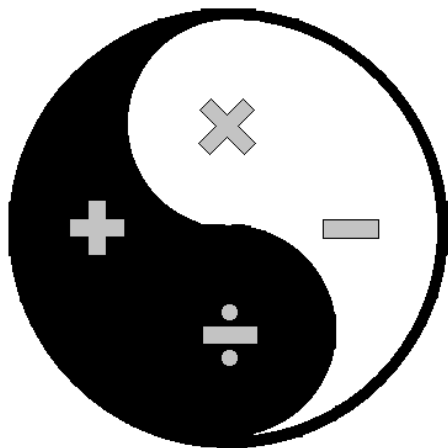
--	--	--	--	--	--	--	--	--	--

3	12
	difference

4	4	4
---	---	---

$$\frac{2}{3} \left(\frac{5}{9}x - 3 \right) = 8$$





The Tai Chi of Basic Mathematics

(An attempt to find balance)

PROBLEM SOLVING Models → Solving an Equation

Given the model and value of the expression, determine the value of its input.

Illustration:

x

The expression has a value of 8; so what is the value of x?

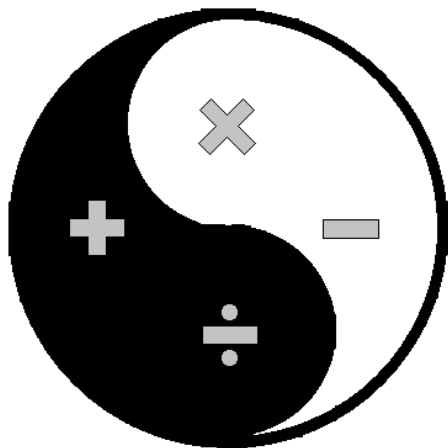
3	3	3	3	3	3	3	3	3
---	---	---	---	---	---	---	---	---

3	12
	difference

4	4	4
---	---	---

$$\frac{2}{3} \left(\frac{5}{9}x - 3 \right) = 8$$





The Tai Chi of Basic Mathematics

(An attempt to find balance)

PROBLEM SOLVING Models → Solving an Equation

Given the model and value of the expression, determine the value of its input.

Illustration:

27

x

The expression has a value of 8; so what is the value of x?

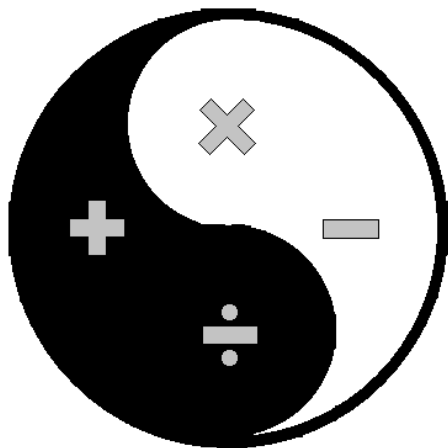
3 3 3 3 3 3 3 3 3

3	12
	difference

4	4	4
---	---	---

$$\frac{2}{3} \left(\frac{5}{9}x - 3 \right) = 8$$





The Tai Chi of Basic Mathematics

(An attempt to find balance)

PROBLEM SOLVING Models → Solving an Equation via the Algebraic Method

Given the model and value of the expression, determine the value of its input.

1) ADD 2 to get 8 for the YELLOW box.

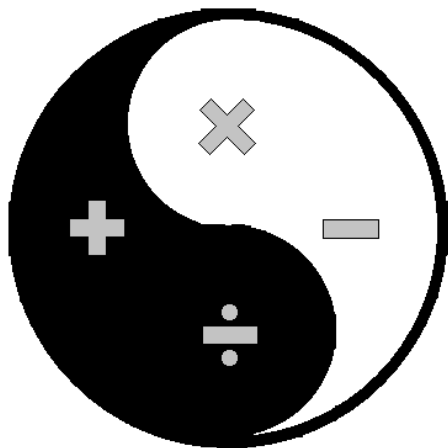
	x			
x	x	x	x	x
1				
	8			
2	6			

$$\frac{(5x - 1)}{3} - 2 = 6$$

Arrows indicate steps: 1 points to $5x$, 2 points to -1 , 3 points to the denominator 3 , and 4 points to the subtraction -2 .

Describe the steps you will need to do to solve for x.





The Tai Chi of Basic Mathematics

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PROBLEM SOLVING Models → Solving an Equation via the Algebraic Method

Given the model and value of the expression, determine the value of its input.

2) MULTIPLY by 3 to get 24

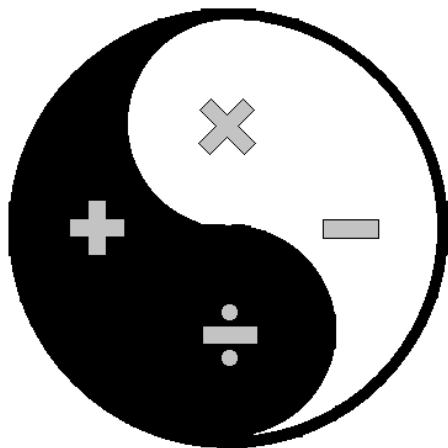
	x			
x	x	x	x	x
1	24			
	8	8	8	
2	6			

$$\frac{(5x - 1)}{3} - 2 = 6$$

Arrows indicate steps: 1 points to $5x$, 2 points to -1 , 3 points to the denominator 3 , and 4 points to the subtraction -2 .

Describe the steps you will need to do to solve for x.





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PROBLEM SOLVING Models → Solving an Equation via the Algebraic Method

Given the model and value of the expression, determine the value of its input.

3) ADD 1 to get 25

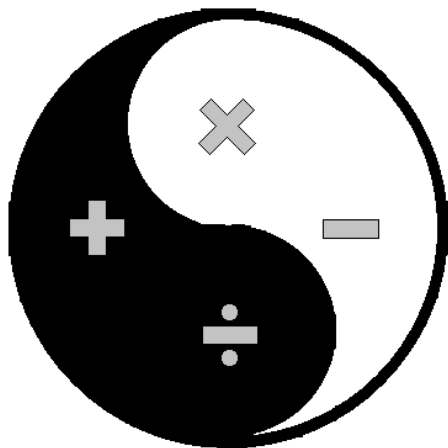
						x
	x	x	x	x	x	
1	24					
	8	8	8			
	2	6				

$$\frac{(5x - 1)}{3} - 2 = 6$$

Arrows indicate steps: 1 points to $5x$, 2 points to -1 , 3 points to the denominator 3 , and 4 points to the subtraction -2 .

25 Describe the steps you will need to do to solve for x.





The Tai Chi of Basic Mathematics

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PROBLEM SOLVING Models → Solving an Equation via the Algebraic Method

Given the model and value of the expression, determine the value of its input.

4) DIVIDE by 5 to get 5

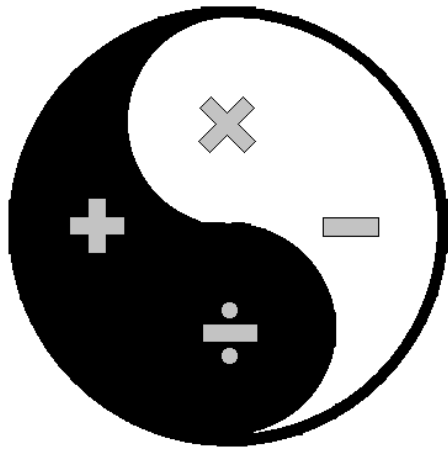
5	x			
x	x	x	x	x
1	24			
8	8	8		
2	6			

$$\frac{(5x - 1)}{3} - 2 = 6$$

Annotations: 1 points to (5x - 1), 2 points to the minus sign in the numerator, 3 points to the denominator 3, 4 points to the minus sign before the 2, 25 points to the entire equation.

Describe the steps you will need to do to solve for x.



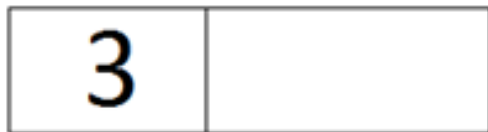


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PROBLEM SOLVING Models → Solving an Equation via the Algebraic Method

Given the model and value of the expression, determine the value of its input.

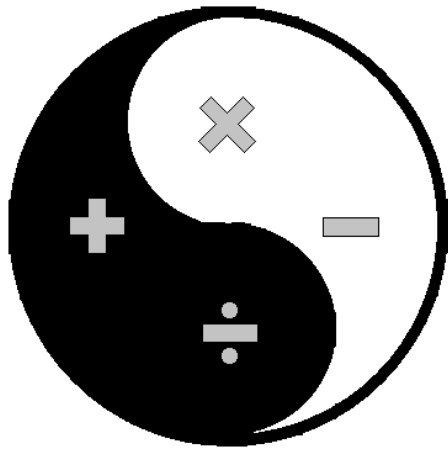


$$2(x - 3) + 5 = 13$$

Arrows point from the numbers 2, 3, and 5 to their respective parts in the equation: 2 points to the coefficient 2, 3 points to the constant 3, and 5 points to the constant 5.

- 1) Subtract 5 from 13 to get the length of the left rectangle.



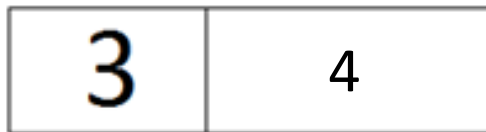


The Tai Chi of Basic Mathematics

(An attempt to find balance)

PROBLEM SOLVING Models → Solving an Equation via the Algebraic Method

Given the model and value of the expression, determine the value of its input.

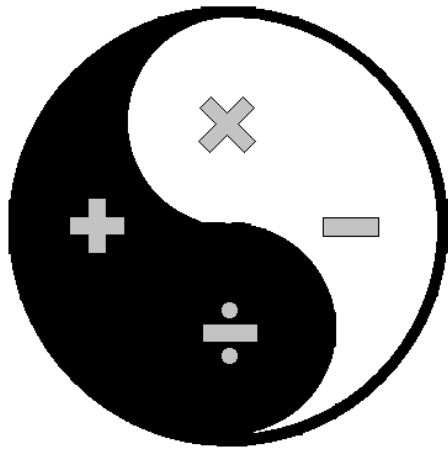


$$2(x - 3) + 5 = 13$$

Diagram illustrating the equation $2(x - 3) + 5 = 13$ with arrows indicating the components: 2 (coefficient), x (variable), 3 (constant), 1 (coefficient of the second term), 5 (constant), and 13 (result).

2) Divide by 2



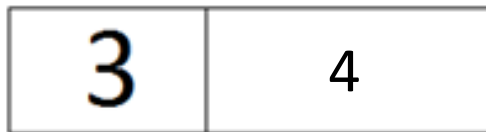
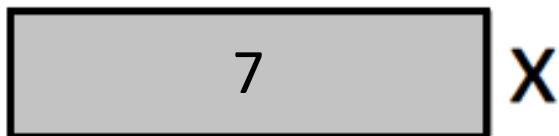


The Tai Chi of Basic Mathematics

(An attempt to find balance)

PROBLEM SOLVING Models → Solving an Equation via the Algebraic Method

Given the model and value of the expression, determine the value of its input.

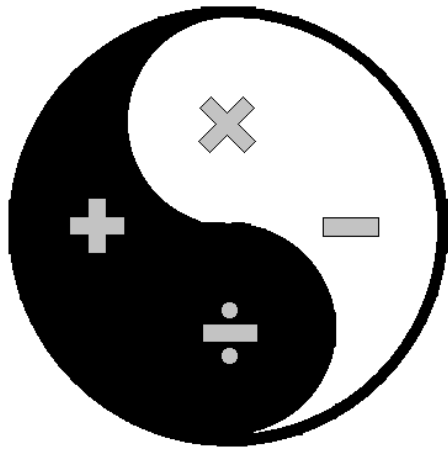


$$2(x - 3) + 5 = 13$$

Diagram illustrating the equation $2(x - 3) + 5 = 13$ with arrows indicating the components: 2 (coefficient), x (variable), 3 (constant), 1 (coefficient), 5 (constant), and 13 (result).

3) Add 3



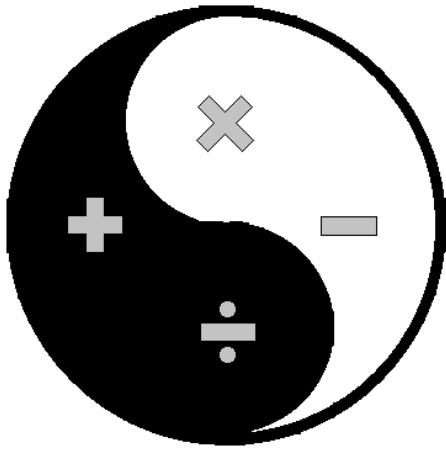


The Tai Chi of Basic Mathematics

(An attempt to find balance)

An Important Goal:

***Problem Solving and
Critical Thinking w/ Applications***



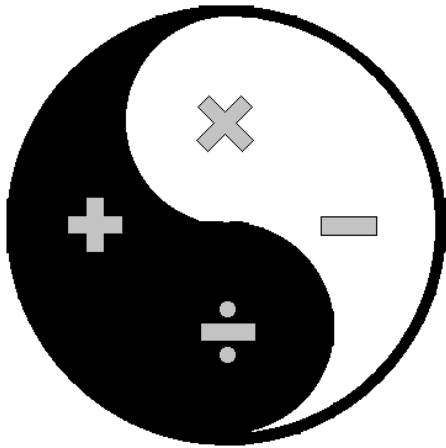
The Tai Chi of Basic Mathematics

(An attempt to find balance)

Jim took \$23.00 with him to go shopping.
His sister, Loretta took \$13.00 **more** than he did.

Jim	\$23.00	more
Loretta		\$13.00

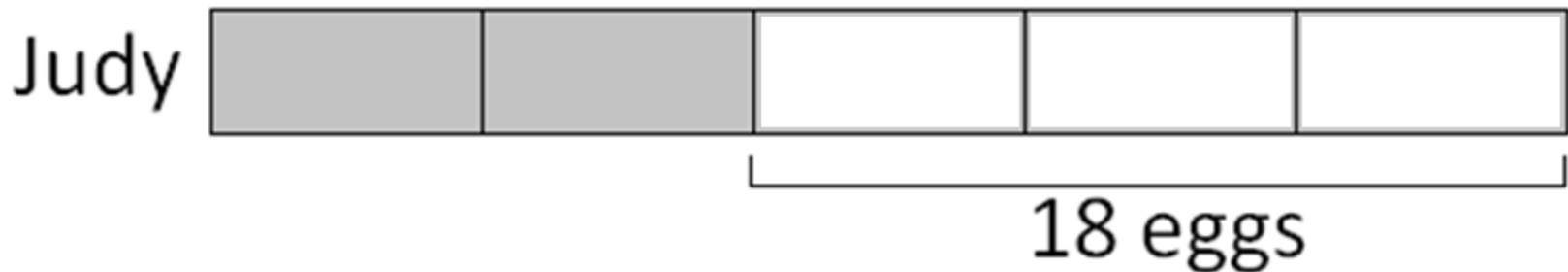
How much did **Loretta** take shopping?



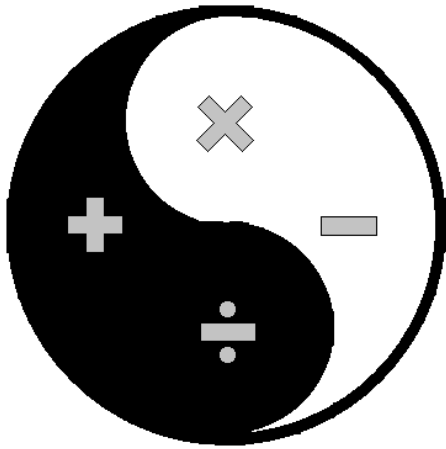
The Tai Chi of Basic Mathematics

(An attempt to find balance)

Judy bought some eggs. She used $\frac{2}{5}$ of the eggs to bake cakes. She had 18 eggs left.



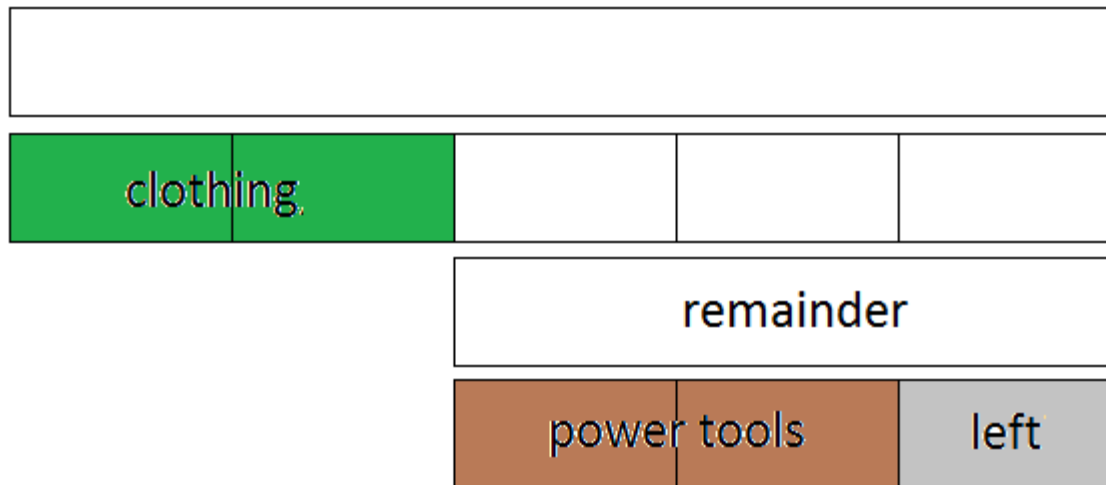
How many eggs did she buy?



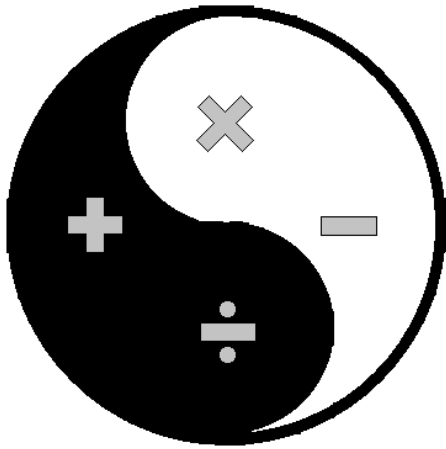
The Tai Chi of Basic Mathematics

(An attempt to find balance)

Tomas took a certain amount of money from his bank account to go shopping at the mall. He spent $\frac{2}{5}$ of the money on clothing, and $\frac{2}{3}$ of the remainder for power tools. What fraction of his original amount was left?



What **fraction** of his original amount was **left**?

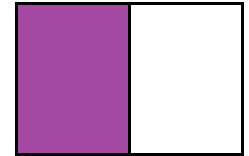
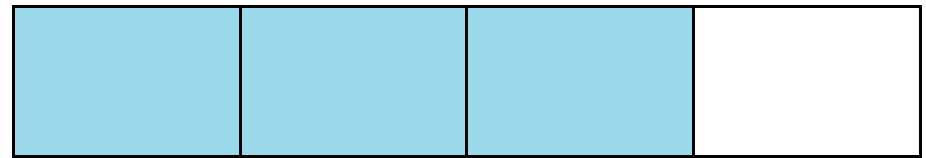


The Tai Chi of Basic Mathematics

(An attempt to find balance)

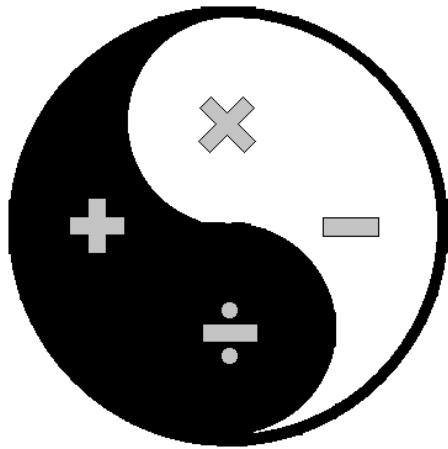
Tom spent **three-quarters** of his money on a dictionary. He spent **one-half of the remainder** on a calculator. The dictionary cost \$30 **more** than the calculator.

How much does the **dictionary** cost?



dictionary cost \$30 more.



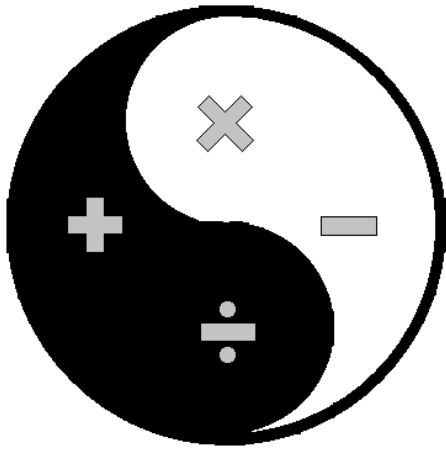


The Tai Chi of Basic Mathematics

(An attempt to find balance)

There are 20 workers in the library. 55% of them were males. **How many fewer females than males** worked in the library?





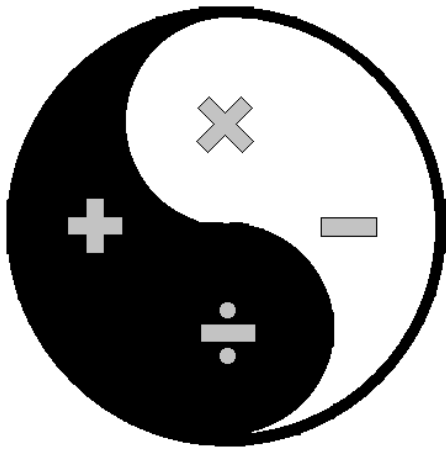
The Tai Chi of Basic Mathematics

(An attempt to find balance)

Mary determined that the population of monarch butterflies at a particular site was 12,000. She estimated that next year there would be a **6% increase** each year.

What would be the estimated population of monarch butterflies **next year**?

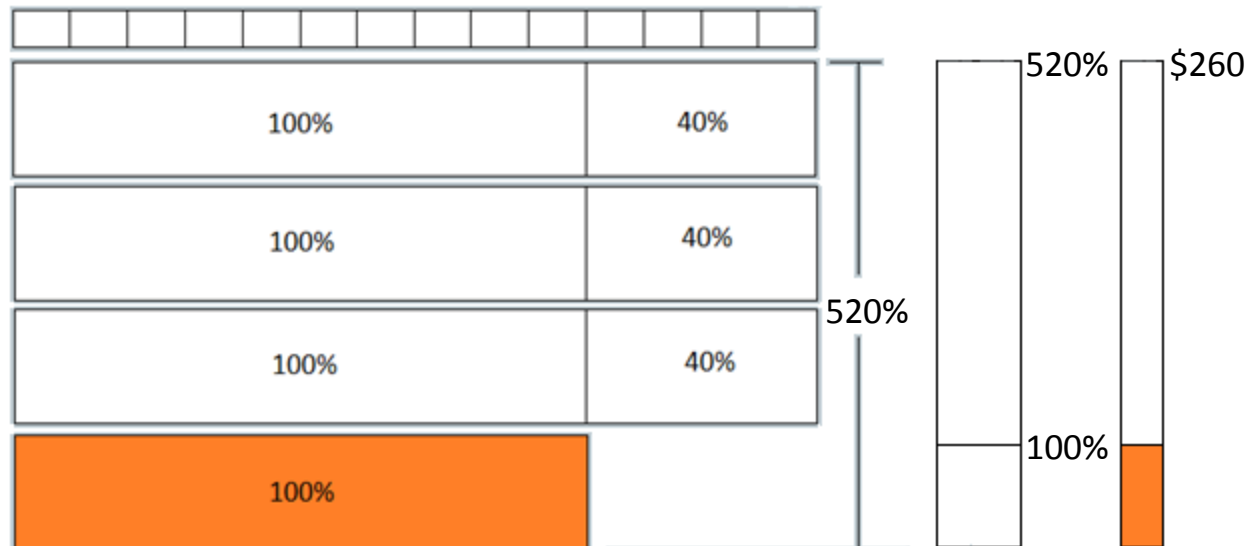
100	6
12,000	?

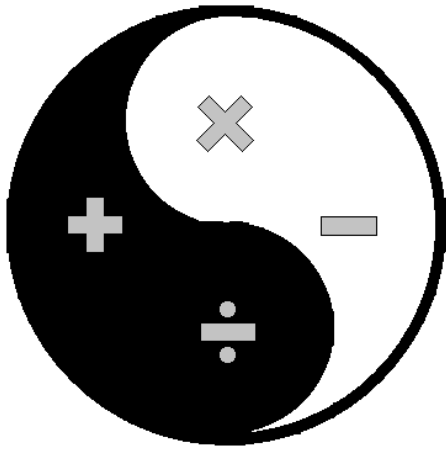


The Tai Chi of Basic Mathematics

(An attempt to find balance)

A shopkeeper had 4 handbags which were of the **same cost price**. He sold 3 of them at **40% more than** the cost price. He sold the fourth handbag at cost price. He received **a total of \$260** altogether. Find the cost price of **each** handbag.



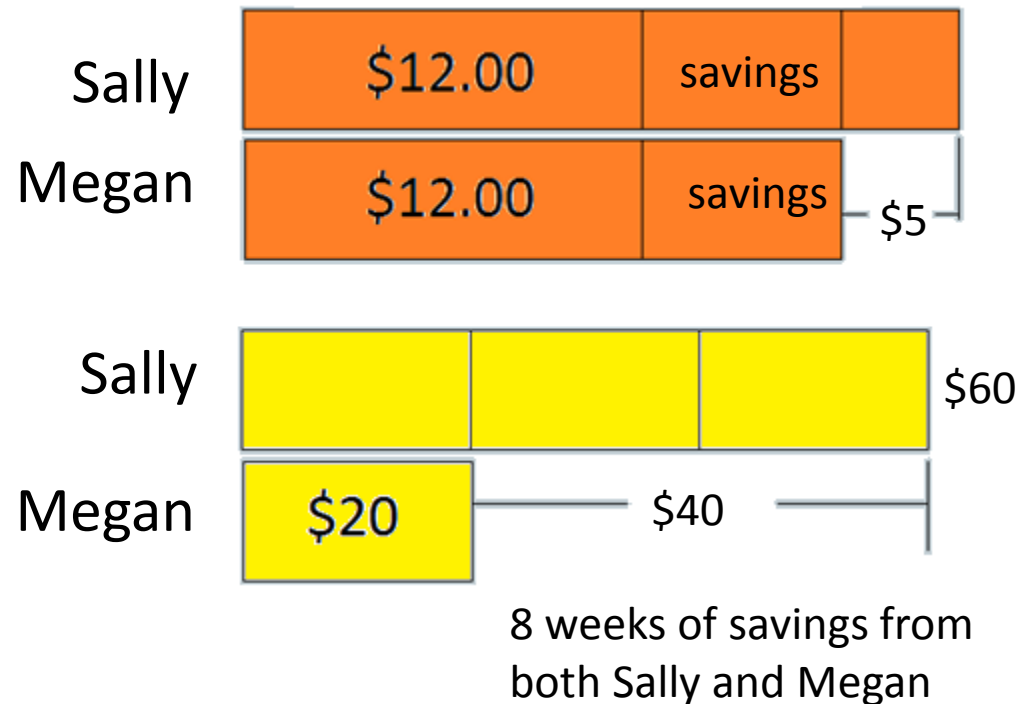


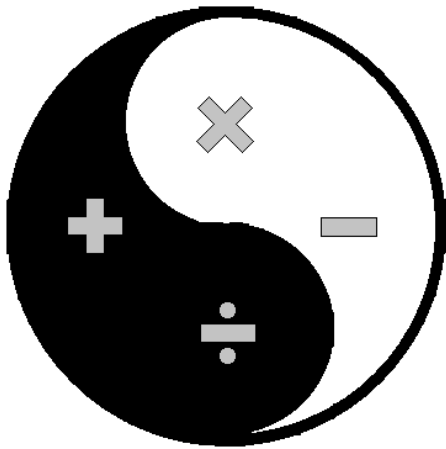
The Tai Chi of Basic Mathematics

(An attempt to find balance)

Sally is given \$5 **more** allowance than Megan each week. They **each spend \$12 per week** and **save the rest**. When **Sally has saved \$60**, **Megan saved \$20**.

Find out **Sally's allowance**.





The Tai Chi of Basic Mathematics

(An attempt to find balance)

In a class, at the beginning of the semester, the **ratio** of girls to boys is 5:3. If an **additional** 4 girls and 12 boys enrolled, there would be the **same** number of girls as boys in the class.

How many girls were there at the beginning of the semester?

Initially,

girls

--	--	--	--	--

boys

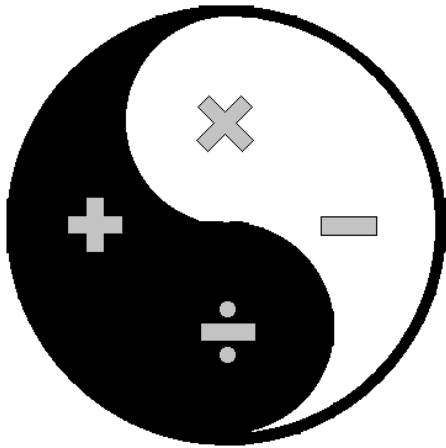
--	--	--

4 additional girls

					4
--	--	--	--	--	---

12 additional boys

			12		
--	--	--	----	--	--

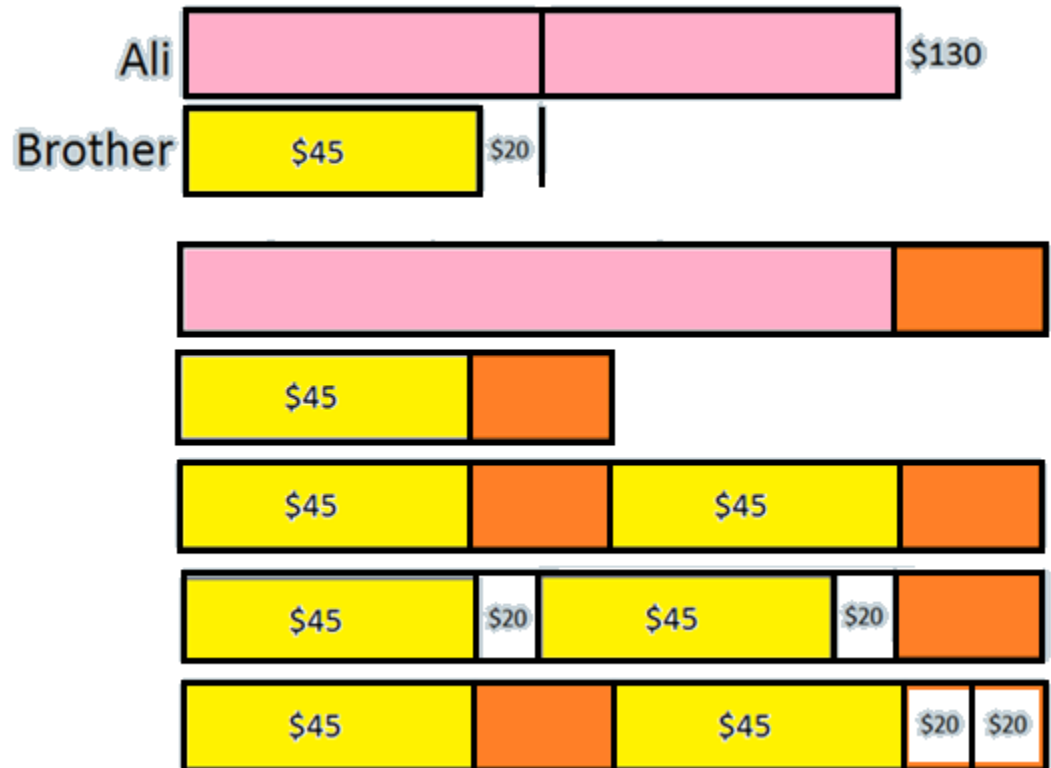


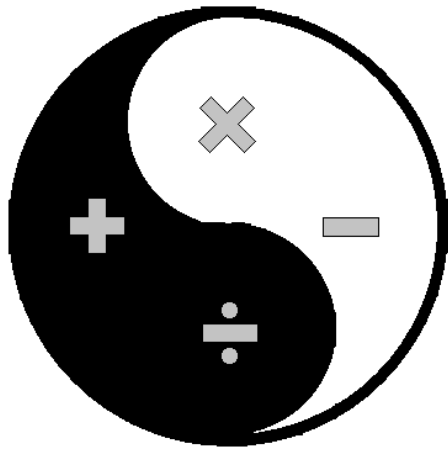
The Tai Chi of Basic Mathematics

(An attempt to find balance)

Ali had \$130 and his brother had \$45. When their mother gave each of them an equal amount of money, Ali had twice as much as his brother.

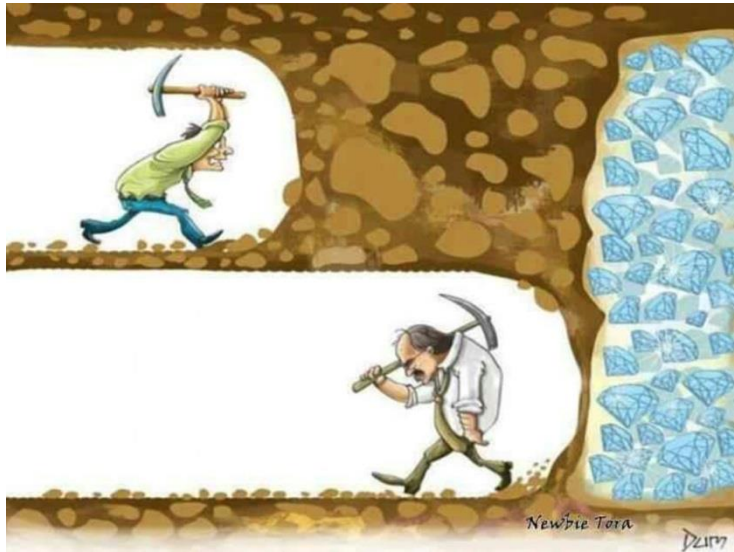
How much did their mother contribute to each of them?





The Tai Chi of Basic Mathematics

(An attempt to find balance)



*Support and
Encourage
Persistence*

Yin Cycle



Yang Cycle

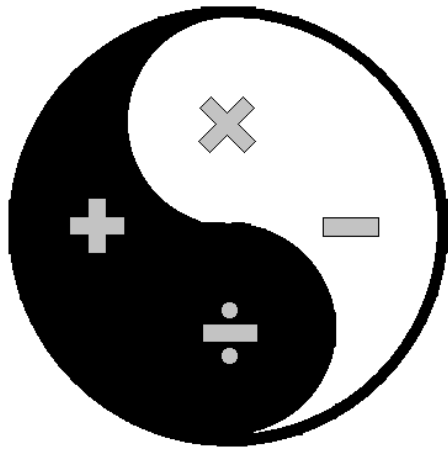
Support Persistence

Avoidance

Behavioral Continuum

Pursuit

Social/
Motivational

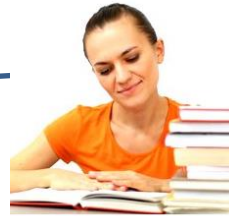


The Tai Chi of Basic Mathematics

(An attempt to find balance)



Solved it and ready to do the next one.



Okay, ready to begin this problem.



It's tougher than I thought!

The vicious elliptical path problem solving . . .

P E R S I S T E N C E



My group mates think that we can get together in the quad to work on it.



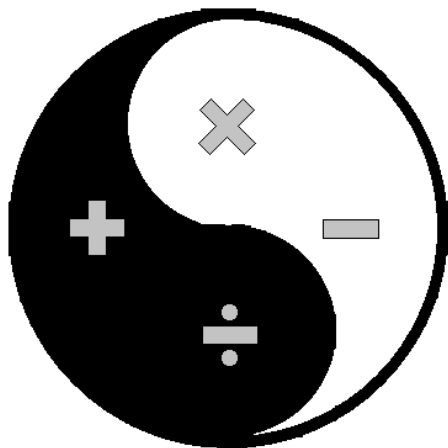
Hey, maybe someone in my class study group can help me?



I've read it over 25 times. Nothing.



I remember now why I hate math.



The Tai Chi of Basic Mathematics

(An attempt to find balance)

ComboReview



Everybody works, everybody benefits.

Half of a Combo-Review (part 1) is taken home giving many students to develop work groups. In class, part 2 with similar objects is given. A master form where answers are recorded when the groups get together is turned in for credit.

