# Blaise Pascal

and his Mystic Hexagram

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# Some Milestones in Pascal's Life

- 1623 Birth (June 19<sup>th</sup>)
- 1639 Presents a paper containing the Mystic Hexagram to Mersenne's group
- 1642 Invents the Pascaline
- 1647 Publishes New Experiments Concerning Vacuums
- 1654 Corresponds with Fermat on the problem of the division of stakes
- 1654 Dedicates himself to religious contemplation
- 1657 Publishes the Provincial Letters
- 1662 Death (August 19<sup>th</sup>)
- 1665 Posthumous publication of the Treatise on the Arithmetic Triangle
- 1669 Posthumous publication of the Pensées

# Some Websites worth exploring

#### How the Pascaline Works

http://www.youtube.com/watch?v=3h71HAJWnVU

#### Pascal's Wager

http://www.iep.utm.edu/pasc-wag/

#### The Complete Pascal Figure

http://www.math.uregina.ca/~fisher/Norma/index.html

Treatise on the Arithmetic Triangle http://www.cs.xu.edu/math/Sources/Pascal/Sources/arith\_triangle.pdf

# **Slides Used in the Presentation:**

http://online.santarosa.edu/homepage/jmartin/ Scroll to the bottom for a link to a folder containing a PDF of the slides.

# **Pascal's Mystic Hexagram**

**Theorem:** If six arbitrary points are chosen on a conic section and joined by line segments in any order to form a hexagon, then the three pairs of opposite sides of the hexagon meet in three points that lie on a straight line.

The complete Pascal figure consists of:

- 60 Pascal lines
- 45 Diagonal points
- 20 Steiner points
- 60 Kirkman points
- 15 Plücker lines
- 20 Cayley lines
- 15 Salmon points

Each diagonal point has 4 Pascal lines. Each Steiner point has 3 Pascal lines. Each Kirkman point has 3 Pascal lines.

Each Pascal line contains

- 3 Diagonal points
- I Steiner point
- 3 Kirkman points
- Each Plücker line contains
  - 4 Steiner points

Each Cayley line contains

- I Steiner point
- 3 Kirkman points

Each Salmon point has 4 Cayley lines